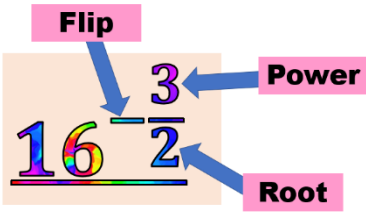
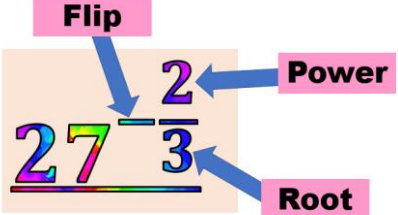
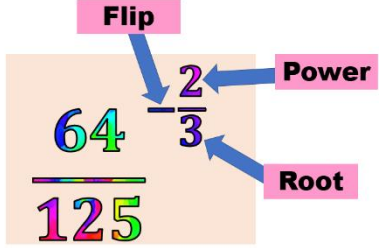


Maths Revision Pack

Year 10 Higher

Assessment Week 1

Name: _____

<u>Example 1</u>	<u>Example 2</u>	<u>Example 3</u>
		
Step 1 : $\sqrt{16} = 4$ Step 2 : $4^3 = 64$ Step 3 : $\frac{1}{64}$	Step 1 : $\sqrt[3]{27} = 3$ Step 2 : $3^2 = 9$ Step 3 : $\frac{1}{9}$	Step 1 : $\sqrt[3]{\frac{27}{125}} = \frac{3}{5}$ Step 2 : $\left(\frac{3}{5}\right)^2 = \frac{9}{25}$ Step 3 : $\frac{25}{9} = 2\frac{7}{9}$

Questions

2^3	3^{-3}	$25^{\frac{1}{2}}$
$25^{-\frac{1}{2}}$	$36^{\frac{1}{2}}$	$27^{\frac{1}{3}}$
$27^{-\frac{1}{3}}$	$64^{\frac{3}{2}}$	$64^{\frac{2}{3}}$
$125^{-\frac{2}{3}}$	$\left(\frac{16}{81}\right)^{\frac{1}{2}}$	$\left(\frac{8}{27}\right)^{-\frac{1}{3}}$
$\left(\frac{49}{121}\right)^{\frac{3}{2}}$	$\left(\frac{9}{144}\right)^{-\frac{3}{2}}$	$\left(\frac{1}{125}\right)^{-\frac{2}{3}}$

<u>Example 1</u>	<u>Example 2</u>	<u>Example 3</u>
<p>Write down $2^7 \times 8$ as a single power of 2.</p> $2^7 \times 8$ $2^7 \times 2^3 = 2^{10}$	<p>Write down $2^5 \times 8^9$ as a single power of 2.</p> $2^5 \times 8^9$ $2^5 \times (2^3)^9$ $2^5 \times 2^{27}$ 2^{32}	<p>Write down $3^7 \times 81^5$ as a single power of 3.</p> $3^7 \times 81^5$ $3^7 \times (3^4)^5$ $3^7 \times 3^{20}$ 3^{27}

Questions

Write these as single a single power

$2^4 \times 16$	$2^9 \times 32$	$3^5 \times 27$
$2^5 \times 8^7$	$2^5 \times 16^3$	$3^2 \times 9^5$
$2^4 \times 8^3$	$4^5 \times 16^9$	$4^2 \times 64^6$
$5^2 \times 25^2$	$5^6 \times 125^4$	$16^3 \times 64^6$
$25^2 \times 125^2$	$9^5 \times 27^2$	$27^2 \times 81^6$

<u>Example 1</u>	<u>Example 2</u>
$(2x^5y^7)^3$ $2x^5y^7 \times 2x^5y^7 \times 2x^5y^7$ $8x^{15}y^{21}$	$(5a^4b^8)^3$ $5a^4b^8 \times 5a^4b^8 \times 5a^4b^8$

Questions

$(6x^4y^7)^2$	$(5x^8y^3)^2$
$(3a^3b^5)^2$	$(7x^3y^9)^2$
$(3x^4y^6)^3$	$(4a^5b^2)^3$

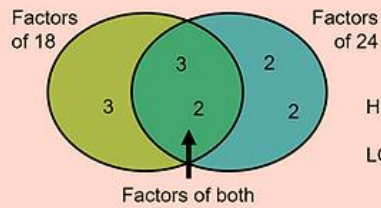
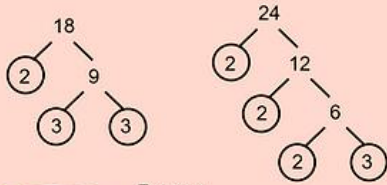
<u>Example 1</u>	<u>Example 2</u>
<div style="border: 1px solid blue; padding: 5px; display: inline-block;"> $9^0 = 1$ $7^2 = 49$ </div> $9^0 \times 7^2$ $1 \times 49 = 49$	<div style="border: 1px solid blue; padding: 5px; display: inline-block;"> $b^0 = 1$ $8^1 = 8$ </div> $b^0 + 8^1$ $1 + 8 = 9$

Questions

$8^1 + 7^0$	$3^2 \times a^0$
$13^0 + 6^2$	$15^1 - 35^0$

Example

Calculate the HCF and LCM of 18 and 24.

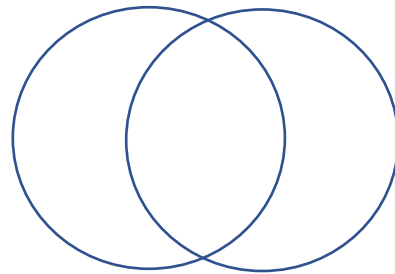


$$\begin{aligned}\text{HCF} &= 2 \times 3 \\ &= 6 \\ \text{LCM} &= 3 \times 2 \times 3 \times 2 \times 2 \\ &= 72\end{aligned}$$

$$\begin{aligned}18 &= \cancel{2} \times 3 \times \cancel{3} \\ 24 &= \cancel{2} \times 2 \times 2 \times \cancel{3}\end{aligned}$$

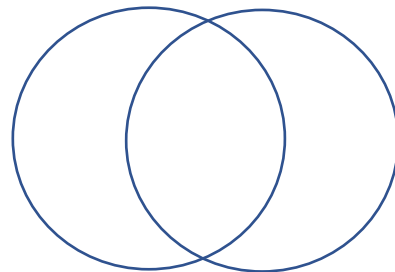
Questions

Find the HCF and LCM of 54 and 36.



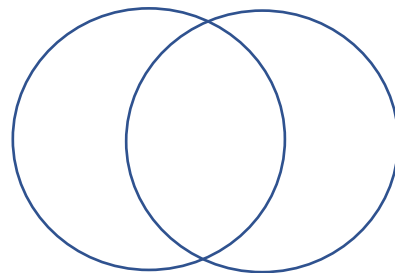
HCF =
LCM =

Find the HCF and LCM of 120 and 220.

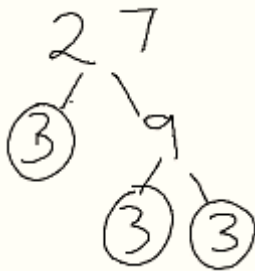


HCF =
LCM =

Find the HCF and LCM of 240 and 180.



HCF =
LCM =

<u>Example 1</u>	<u>Example 2</u>	<u>Example 3</u>
$N = 3^4 \times 5^3 \times 7^5$ What is $3N$? $3 \times 3^4 \times 5^3 \times 7^5$ $= 3^5 \times 5^3 \times 7^5$	$N = 2^3 \times 3^3 \times 5^2$ What is $3N^2$? $3 \times 2^3 \times 3^3 \times 5^2 \times 2^3 \times 3^3 \times 5^2$ $2^6 \times 3^7 \times 5^4$	$N = 2^3 \times 3^8 \times 5^2$ What is $27N^2$?  $27 = 3^3$ $3^3 \times 2^3 \times 3^8 \times 5^2 \times 2^3 \times 3^8 \times 5^2$ $2^6 \times 3^{11} \times 5^4$

Questions

$N = 2^4 \times 5^3 \times 7^5$ What is $5N$?	$N = 2^3 \times 3^3 \times 5^2$ What is $2N^2$?	$N = 2^3 \times 3^8 \times 5^2$ What is $24N^2$?
$N = 3^4 \times 5^3 \times 7^5$ What is $2N$?	$N = 2^9 \times 3^3 \times 7^2$ What is $3N^2$?	$N = 2^3 \times 3^7 \times 5^2$ What is $18N^2$?
$N = 2^7 \times 3^8 \times 5^3 \times 7^5$ What is $7N$?	$N = 2^5 \times 3^8 \times 5^3 \times 7^5$ What is $5N^2$?	$N = 2^4 \times 3^8 \times 5^2$ What is $125N^2$?

Example 1

SOLVE FOR X:

$$15 + 6x = 45 + 8x$$

$$\begin{array}{r} 15 + 6x = 45 + 8x \\ -6x \quad -6x \end{array}$$

$$15 = 45 + 2x$$

$$-45 \quad -45$$

$$-30 = 2x$$

$$\frac{-30}{2} = \frac{2x}{2}$$

$$-15 = x$$

Check your answer:

$$15 + 6(-15) \stackrel{?}{=} 45 + 8(-15)$$

$$15 + (-90) \stackrel{?}{=} 45 + (-120)$$

$$-75 = -75 \quad \checkmark$$

Example 2

$$\frac{2x}{5} = 3$$

Add a one underneath to make it a fraction

$$\frac{2x}{5} = \frac{3}{1}$$

Fraction=fraction
Use scissors

$$2x(1) = 3(5)$$

$$2x = 15$$

$$\frac{2x}{2} = \frac{15}{2}$$

$$x = \frac{15}{2} = 7\frac{1}{2}$$

Example 3

$$\frac{3w+4}{5} = \frac{2}{7}$$

Fraction=fraction
Use scissors

$$7(3w+4) = 5(2)$$

$$21w + 28 = 10$$

$$(-28) \quad (-28)$$

$$\frac{21w}{21} = \frac{-18}{21}$$

$$w = \frac{-18}{21}$$

Example 4

Fractions Both Sides Equation

Solve the Equation : $\frac{8h+7}{2} = 3h-4$

1a. Cross Multiply : $8h+7 \rightarrow 3h-4$

$$\frac{8h+7}{2} = \frac{3h-4}{1}$$

1b. Use Brackets : $1(8h+7) = 2(3h-4)$

1c. Expand Out : $8h+7 = 6h-8$

Now solve as letter both sides

Questions

Solve these equations

$$\frac{x}{4} = 8$$

$$\frac{2a}{3} = 8$$

$$\frac{10x-1}{7} = 8$$

$$\frac{7c + 4}{8} = 11$$

$$\frac{53 - 2x}{5} = 7$$

$$\frac{11 - w}{5} = 3 + w$$

$$\frac{9(4x - 1)}{2x} = 15$$

$$\frac{x}{2x - 1} = 5$$

$$\frac{2(3x - 6)}{5} = \frac{3x}{2}$$

$$\frac{x + 15}{3} = 2(x + 10)$$

$$\frac{5x}{5} = 3x - 8$$

$$2(5 - 6x) = \frac{3x}{2}$$

Example 1

$$\frac{3x}{5} + 2 = 7$$

(-2) (-2)

$$\frac{3x}{5} = 5$$

$$\frac{3x}{5} \times \frac{5}{1}$$

$$1(3x) = 5(5)$$

$$3x = 25$$

$$x = \frac{25}{3}$$

Add a one
underneath to
make it a fraction

Fraction=fraction
Use scissors

Example 2

$$\frac{4}{5w} + 1 = 12$$

(-1) (-1)

$$\frac{4}{5w} = 11$$

$$\frac{4}{5w} \times \frac{1}{1}$$

$$4(1) = 5w(11)$$

$$4 = 55w$$

$$w = \frac{4}{55}$$

Add a one
underneath to
make it a fraction

Fraction=fraction
Use scissors

Solve these equations

$$\frac{x}{2} + 1 = 3$$

$$\frac{a}{3} + 4 = 9$$

$$\frac{2r}{5} - 3 = 2$$

$$\frac{3}{c} + 8 = 2$$

$$\frac{3x}{4} + 1 = 12$$

$$\frac{4}{p} + 3 = 5$$

Example 1

$$\frac{2x^{x^2}}{3x^2} + \frac{4x-1}{2x^3} = 5$$
$$\frac{2(2x)}{6} + \frac{3(4x-1)}{6} = 5$$
$$\frac{4x}{6} + \frac{12x-3}{6} = 5$$
$$\frac{16x-3}{6} = 5$$

Make the
denominators
the same.

Fraction=fraction
scissors

$$1(16x-3) = 5(6)$$
$$16x-3 = 30$$
$$(+3) \quad (+3)$$
$$\frac{16x}{16} = \frac{33}{16}$$
$$x = \frac{33}{16}$$

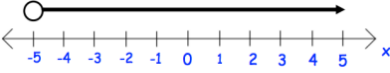
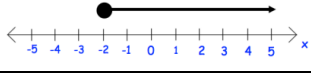
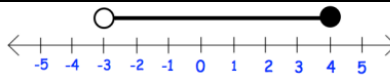
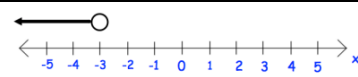


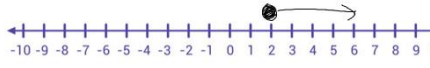
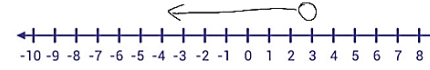


Solve these equations

$$\frac{x+5}{3} + \frac{x+1}{2} = 8$$

$$\frac{2x-1}{4} + \frac{x-3}{5} = 3$$

$$\frac{x+5}{10} - \frac{x+4}{2} = 1$$

$$\frac{x-3}{4} - \frac{x-8}{3} = 4$$

Examples		
<p>● Includes the number</p> <p>○ Does not Include the</p>	 <p>x is more than -5</p>	 <p>x is more than or equal to -2</p>
<p>< or > ○</p> <p>≤ or ≥ ●</p>	 <p>x is more than -3 but less than or equal to 4</p>	 <p>x is less than -3</p>
<p>Solve:</p> $5x + 3 < 15$ <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> $\begin{array}{r} 5x + 3 < 15 \\ (-3) \quad (-3) \\ \hline 5x < 12 \\ \frac{5x}{5} < \frac{12}{5} \\ x < 2.4 \end{array}$ </div> <p>x is less than 3</p>  <p>2,1,0,-1,-2.....</p>	<p>Solve:</p> $4(2x - 3) \geq 28$ <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> $\begin{array}{r} 4(2x - 3) \geq 28 \\ 8x - 12 \geq 28 \\ (+12) \quad (+12) \\ \hline 8x \geq 40 \\ \frac{8x}{8} \geq \frac{40}{8} \\ x \geq 5 \end{array}$ </div> <p>x is more than or equal to 5</p>  <p>5,6,7,8,9,10,11.....</p>	$\frac{8x - 4}{3} \geq 4$ $\frac{8x - 4}{3} \geq \frac{4}{1}$ $1(8x - 4) \geq 3(4)$ $8x - 4 \geq 12$ $(+4) \quad (+4)$ $\frac{8x}{8} \geq \frac{16}{8}$ $x \geq 2$  <p>2,3,4,5,6,7,8.....</p>
$\frac{8x}{3} - 4 < 4$ $\frac{8x}{3} - 4 < 4$ $(+4) \quad (+4)$ $\frac{8x}{3} < 8$ $\frac{8x}{3} < \frac{8}{1}$ $1(\frac{8x}{3}) < 3(8)$ $\frac{8x}{8} < \frac{24}{8}$ $x < 3$  <p>2,1,0,-1,-2.....</p>	<p>Solve:</p> $5x + 3 \leq 2x + 33$ $5x + 3 \leq 2x + 33$ $(-2x) \quad (-2x)$ $3x + 3 \leq 33$ $(-3) \quad (-3)$ $\frac{3x}{3} \leq \frac{30}{3}$ $x \leq 10$  <p>10,9,8,7,6,5,4.....</p>	<p>Solve:</p> $-12 \leq 5x + 3 < 33$ <div style="border: 1px solid black; padding: 5px; margin: 10px 0;"> $\begin{array}{r} -12 \leq 5x + 3 < 33 \\ (-3) \quad (-3) \quad (-3) \\ \hline -15 \leq 5x < 30 \\ \frac{-15}{5} \leq \frac{5x}{5} < \frac{30}{5} \\ -3 \leq x < 6 \end{array}$ </div> <p>x is more than or equal to -3 but less than 6</p>  <p>-3,-2,-1,0,1,2,3,4,5</p>
<h1>Questions</h1>		
<p>Solve these inequalities, draw a number line and write down the integers that satisfy the inequalities.</p>		

$2x + 1 \leq 9$	$3x - 5 > 16$	$4(2x + 1) > 9$
$5x - 2 \geq 68$	$4x \leq x + 6$	$\frac{x}{9} - 6 > 4$
$\frac{x}{2} + 1 \leq 5$	$\frac{x + 3}{2} \geq 5$	$\frac{x - 5}{4} > 2$
$\frac{x + 18}{4} \leq 5$	$4x + 6 \leq x + 21$	
$9x + 4 > 7x + 15$	$4x - 4 \leq 7x - 19$	
$5 < 2y < 12$	$4 \leq 2x \leq 8$	
$-3 \leq x + 2 < 2$	$1 \leq 2y - 3 < 9$	
$16 \leq 5x + 1 < 31$	$7 < 2y - 3 \leq 25$	

Example1

$$y = 2x + 1$$

x	-1	0	1	2	3
y	-1	1	3	5	7

$$2(3) + 1 = 7$$

$$2(2) + 1 = 5$$

$$2(1) + 1 = 3$$

$$2(0) + 1 = 1$$

$$2(-1) + 1 = -1$$

Example2

$$x + 2y = -2$$

x	-1	0	1	2	3
y	-0.5	-1	-1.5	-2	-2.5

$$-1 - \frac{1}{2}(3) = -2.5$$

Re-arrange to make y the subject

$$-1 - \frac{1}{2}(2) = -2$$

$$-1 - \frac{1}{2}(1) = -1.5$$

$$-1 - \frac{1}{2}(0) = -1$$

$$-1 - \frac{1}{2}(-1) = -0.5$$

$$x + 2y = -2$$

(-x) (-x)

$$2y = \frac{-2 - x}{2}$$

$$y = -1 - \frac{1}{2}x$$

Questions

$$y = 3x - 1$$

x	-1	0	1	2	3
y	-4			5	

$$y = 4x - 2$$

x	-2	-1	0	1	2	3
y						

$$y = \frac{1}{2}x + 1$$

x	-2	-1	0	1	2	3	4
y							

$$2x + y = 4$$

x	-1	0	1	2	3
y					

Example1

Gradients from two points

Find the gradient of the line passing through (2,5) and (6,13)

TSD: Two coordinates
Subtract
Divide

Find the gradient of the line passing through (2,5) and (6,13)

$$\frac{y}{x} = \frac{8}{4} = 2$$
$$\begin{array}{r} 6, 13 \\ - 2, 5 \\ \hline 4, 8 \end{array}$$

Gradient = 2

Example2

Gradients from two points

Find the gradient of the line passing through (-2,9) and (-4,7)

TSD: Two coordinates
Subtract
Divide

Find the gradient of the line passing through (-2,9) and (-4,7)

$$\frac{y}{x} = \frac{2}{2} = 1$$
$$\begin{array}{r} -2, 9 \\ - -4, 7 \\ \hline 2, 2 \end{array}$$

(-2) - (-4) = 2

Gradient = 1

Questions

(1, 4) and (3, 10)

(0, 0) and (3, 12)

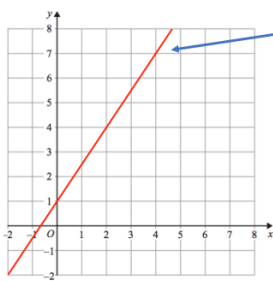
(5, -2) and (9, 14)

(-5, -9) and (1, 3)

(-7, -2) and (1, -4)

(-2, 1) and (8, -7)

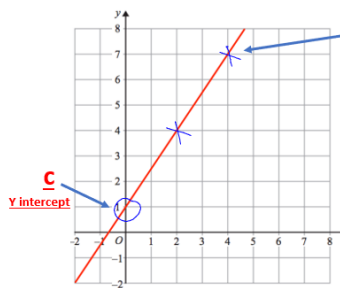
Example



Straight line
 $Y = mx + c$

Gradient

TSD: Two coordinates
Subtract
Divide



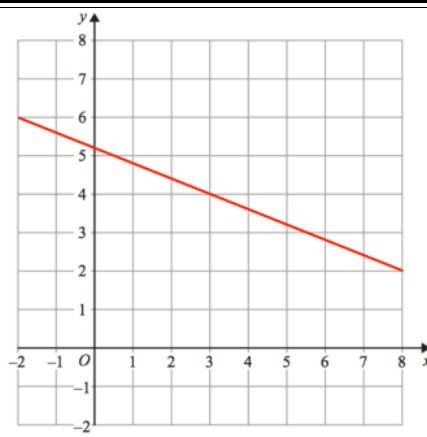
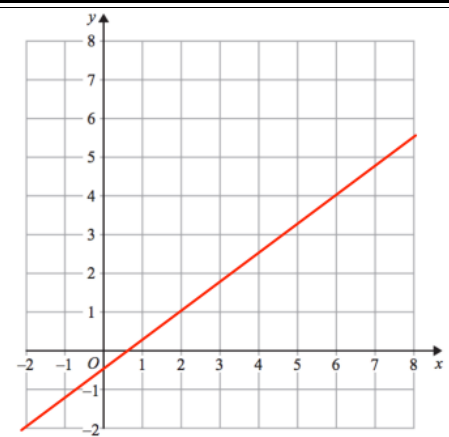
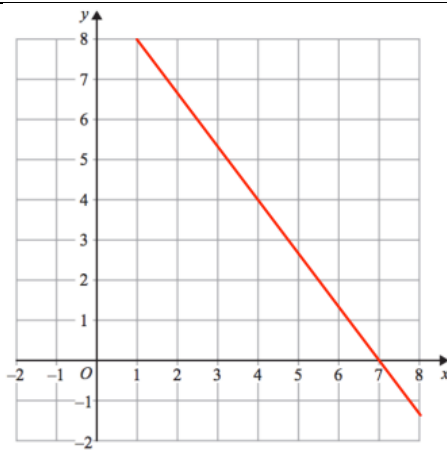
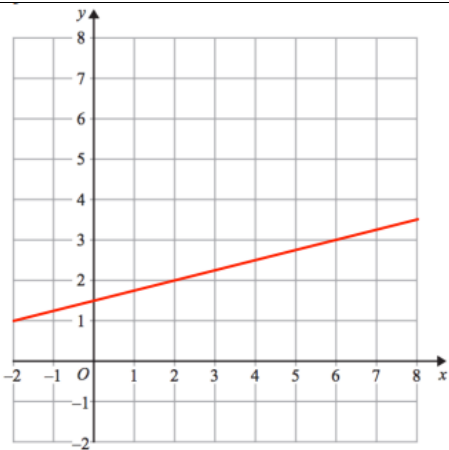
TSD: Two coordinates
Subtract
Divide

$$\frac{4-1}{2-0} = \frac{3}{2}$$

Gradient (m) = $\frac{3}{2}$
Y-intercept (c) = 1

Equation: $y = \frac{3}{2}x + 1$

Questions: find the equations



Example1

Find the equation of the line passing through (2,5) and (4,11)

$Y = mx + c$ Y intercept

Gradient

TSD: Two coordinates
Subtract
Divide

Find the equation of the line passing through (2,5) and (4,11)

$\frac{y}{x} = \frac{6}{2} = 3$

Sub in

$y = 3x + c$
 $11 = 3(4) + c$
 $11 = 12 + c$
 $c = -1$

Gradient (m) = 3
Y-intercept (c) = -1
Equation: $y = 3x - 1$

Example2

Find the equation of the line passing through (-5,-8) and (-4,-4)

$Y = mx + c$ Y intercept

Gradient

TSD: Two coordinates
Subtract
Divide

Find the equation of the line passing through -5,-8 and (-4,-4)

$\frac{y}{x} = \frac{-4}{-1} = 4$

Sub in

$y = 4x + c$
 $-4 = 4(-4) + c$
 $-4 = -16 + c$
 $+16 \quad +16$
 $c = 12$

Gradient (m) = 4
Y-intercept (c) = 12
Equation: $y = 4x + 12$

Questions: find the equations

(1, 6) and (5, 4)

(3, 5) and (4, 1)

(-4, 2) and (1, 7)

(-5, 4) and (5, 2)

(-6, -4) and (-3, 2)

(-10, -5) and (-7, 4)

Examples	
<p>The equation of line L_1 is $y = 5x + 1$</p> <p>The equation of line L_2 is $2y - 10x + 3 = 0$</p> <p>Show that these two lines are parallel.</p>	<p>Parallel \rightarrow Same gradient (m)</p> <p>Re-arrange $y = mx + c$</p> <p>L_1 $y = 5x + 1$ $m = 5$</p> <p>L_2 $2y - 10x + 3 = 0$ Same gradient $(+10x) \quad (+10x)$ $2y + 3 = 10x$ $(-3) \quad (-3)$ $2y = 10x - 3$ $\frac{2y}{2} = \frac{10x - 3}{2}$ $y = 5x - \frac{3}{2}$ $m = 5$</p>
<p>Parallel to $y = 6x + 3$ and passing through $(10, 5)$</p>	<p>Parallel to $y = 6x + 3$ and passing through $(10, 5)$</p> <p>Parallel m is also 6 $m = 6$</p> <p>Same gradient $y = 6x + c$</p> <p>$5 = 6(10) + c$</p> <p>$5 = 60 + c$ $(-60) \quad (-60)$ $-55 = c$</p> <p>$y = 6x - 55$</p>
<p>Find the equation of the straight line passing through the point $(0, 1)$ which is perpendicular to the line $y = -2x + 2$</p>	<p>Perpendicular \rightarrow Change sign & Flip gradient</p> <p>$y = -2x + 2$ $m = -2$</p> <p>* Perpendicular gradient = $+\frac{1}{2}$ $(x, y) (0, 1)$</p> <p>$y = \frac{1}{2}x + c$ \leftarrow Sub in</p> <p>$1 = \frac{1}{2}(0) + c$ $1 = 0 + c$ $c = 1$ $y = \frac{1}{2}x + 1$</p>

Questions

<p>Find the equation of the line that is parallel to $y = \frac{1}{2}x - 3$ and passes through the point $(6, -2)$.</p>	<p>Parallel to $y = 5x - 4$ and passing through $(2, 9)$</p>
<p>Parallel to $y = 4x$ and passing through $(-1, 3)$</p>	<p>Perpendicular to $y = -3x + 4$ and passing through $(6, 1)$</p>

<p>Examples</p>	
<p>$a:b = 2:5$ What fraction is b?</p> <p>$a:b$ Total $2:5$ 7</p> <p>$b = \frac{5}{7}$</p>	<p>$\frac{5}{9}$ of the apples are green. The rest are red. Write down the ratio of red : green</p> <p>Write down the ratio of green : red</p> <p>$\frac{5}{9} = \text{Green}$ (Green arrow from 5, Total arrow from 9)</p> <p>$R:G$ Total $G:R$ Total $4:5$ 9 $5:4$ 9</p>
<p>Amy and Ben share some money. Amy gets four times as much as Ben. Write down the ratio of Amy : Ben</p> <p>Amy : Ben $4 : 1$ x4</p>	<p>Write $4:7$ in the form of $n:1$</p> <p>$4:7 \div 7 \rightarrow \frac{4}{7} : 1$</p> <p>Write $4:7$ in the form of $1:n$</p> <p>$4:7 \div 4 \rightarrow 1 : \frac{7}{4}$</p>
<p>$a:b = 2:5$ $a + b = 21$. what is $a - b$?</p> <p>$a:b$ Total $2:5$ 7</p> <p>x3 x3 x3 $6:15$ 21</p> <p>$a+b=21$ Total</p> <p>$\frac{21}{7} = 3$</p>	<p>$a:b = 2:5$ $b - a = 21$, what is $b + a$?</p> <p>$a:b$ Total $2:5$ 7</p> <p>x7 x7 x7 14 21 35 49</p> <p>$b-a=21$ difference in parts</p>
<p>Amy and Ben share some money in the ratio $4:9$. Amy gets £35 less than Ben. How much did they share?</p> <p>A : B Total $4:9$ 13</p> <p>x7 x7 x7 28 35 63 91</p> <p>£35 less than means $B-A$ difference in parts</p>	<p>$a:b = 7:4$ $b:c = 2:5$</p> <p>Work out $a:c$ Give your answer in its simplest form.</p> <p>$a:b$ $b:c$ $7:4$ $2:5$</p> <p>x1 x1 x2 x2 $\frac{7}{4}$ $\frac{4}{4}$ $\frac{10}{4}$</p> <p>LCM of 4 & 2 15 4</p> <p>$a:c$ $7:10$</p>
<p>$a:b$ is $4:9$. Write down an equation</p> <p>$3:9$ simplifies to $1:3$</p> <p>$3 \times 3 = 1 \times 9$ $9 = 9$</p> <p>$a:b$ $4:9$</p> <p>$9a = 4b$</p>	<p>$8x = 3y$ Write down the ratio of $x:y$</p> <p>$8x = 3y$</p> <p>$x:y$ $3:8$</p>

<p>Jamie and Alastair share some sweets in the ratio 7 : 5. Jamie gives 2 sweets to Alastair. The ratio of sweets is now 13 : 11.</p> <p>How many sweets did each initially have?</p> <p>J : A</p> <p>before $7x : 5x$</p> <p>Now $7x-2 : 5x+2$</p> <p>Now $13 : 11$</p> $11(7x-2) = 13(5x+2)$ $77x-22 = 65x+26$ $+22 \quad +22$ $77x = 65x+48$ $-65x \quad -65x$ $12x = 48$ $\frac{12x}{12} = \frac{48}{12}$ $x = 4$	<p>The ratio of green to yellow beads is 4 : 5, and there are initially 27 beads. I add some yellow beads and the ratio is now 1 : 3. How many yellow beads did I add?</p> <p>G : Y Total</p> <p>4 : 5 9</p> <p>$\times 3 \quad \times 3 \quad \times 3$</p> <p>before 12 : 15 27</p> <p>Now 12 : 15+x</p> <p>Now 1 : 3</p> <p>$3(12) = 1(15+x)$</p> <p>$36 = 15+x$</p> <p>$-15 \quad -15$</p> <p>$21 = x$</p> <p>$\frac{27}{9} = 3$</p>
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Questions

<p>a:b = 3:5</p> <p>What fraction is b?</p>	<p>$\frac{8}{9}$ of the apples are green. The rest are red.</p> <p>Write down the ratio of red : green</p> <p>Write down the ratio of green : red</p>
<p>Amy and Ben share some money. Ben gets five times as much as Amy.</p> <p>Write down the ratio of Amy : Ben</p>	<p>Write 3:8 in the form of n:1</p> <p>Write 3:8 in the form of 1:n</p>
<p>a:b = 3:5</p> <p>a + b = 32. what is a – b?</p>	<p>a:b = 3:5</p> <p>b – a = 32, what is b + a?</p>
<p>Amy and Ben share some money in the ratio 5:8.</p> <p>Amy gets £33 less than Ben. How much did they share?</p>	<p>a, b and c are positive integers.</p> <p>a : b = 3 : 8 and b : c = 6 : 11</p> <p>Work out the smallest possible value of a + b + c</p>
<p>a : b is 4:9. Write down an equation</p>	<p>$8x = 3y$ Write down the ratio of x:y</p>
<p>The ratio of the number of boys to girls at a party is 3 : 4</p> <p>Six boys leave the party.</p> <p>The ratio of the number of boys to girls at the party is now 5 : 8</p> <p>Work out the number of girls at the party.</p>	<p>The ratio of red to blue counters is 2 : 5 and there are 40 blue counters. When I remove some red counters the ratio is now 1 : 4. How many red counters did I remove?</p>

Examples

$$x^2 - 7x + 12$$

$$ax^2 + bx + c$$

$$x^2 - 7x + 12$$

$$(x-3)(x-4)$$

$$a=1$$

$$b=-7$$

$$c=12$$

		ac
x		12
	-3	-4
	-7	
	b	

• 1x12
• 2x6
• 3x4

$$x^2 + 4x - 5$$

$$ax^2 + bx + c$$

$$x^2 + 4x - 5$$

$$(x+5)(x-1)$$

$$a=1$$

$$b=4$$

$$c=-5$$

		ac
x		-5
	5	-1
	4	
	b	

• 1x5

$$x^2 - 81$$

difference of two squares.

$$x^2 - 81$$

$$(x+9)(x-9)$$

$$2x^2 + 7x - 15$$

$$ax^2 + bx + c$$

$$2x^2 + 7x - 15$$

$$2x^2 + 10x - 3x - 15$$

$$2x(x+5) - 3(x+5)$$

$$(2x-3)(x+5)$$

$$a=2$$

$$b=7$$

$$c=-15$$

		ac
x		-30
	10	-3
	7	
	b	

• 1x30
• 2x15
• 3x10
• 5x6

$$\frac{20x^2 + 21x + 4}{16x^2 - 1}$$

$$ax^2 + bx + c$$

$$20x^2 + 21x + 4$$

$$20x^2 + 5x + 16x + 4$$

$$5x(4x+1) + 4(4x+1)$$

$$(5x+4)(4x+1)$$

$$a=20$$

$$b=21$$

$$c=4$$

		ac
x		80
	5	16
	21	
	b	

• 1x80
• 2x40
• 4x20
• 5x16

difference of 2 squares

$$16x^2 - 1$$

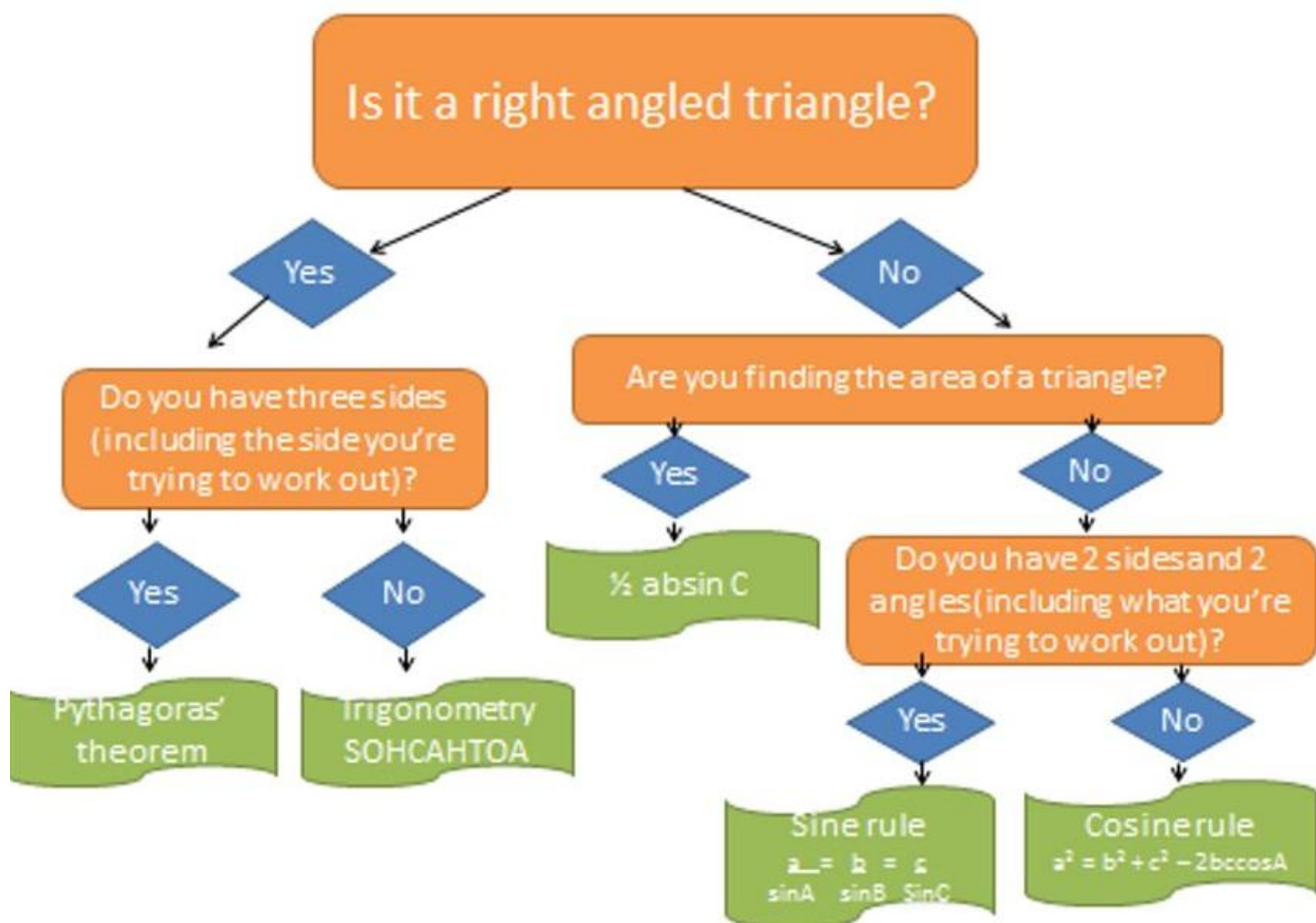
$$(4x+1)(4x-1)$$

$$\frac{(5x+4)(4x+1)}{(4x+1)(4x-1)}$$

$$= \frac{5x+4}{4x-1}$$

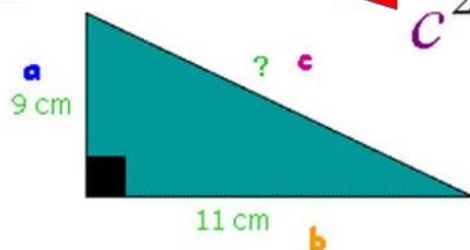
Factorise: $2w + 6$	$2w + 6$ $HCF = 2$ $2(w + 3)$
Factorise: $w^2 - 16$	$w^2 - 16$ $(w + 4)(w - 4)$ <i>← difference of 2 squares</i>
Factorise: $w^2 + 4w + 3$	$w^2 + 4w + 3$ $(w + 1)(w + 3)$ $a = 1$ $b = 4$ $c = 3$ <div style="display: inline-block; vertical-align: middle; text-align: center;"> $\begin{array}{ c c } \hline \times & 3 \\ \hline 1 & 3 \\ \hline + & 4 \\ \hline \end{array}$ </div>
Simplify $\frac{2x + 8}{x^2 - 16}$	$2x + 8 = 2(x + 4)$ $x^2 - 16 = (x + 4)(x - 4)$ $\frac{2(x + 4)}{(x + 4)(x - 4)} = \frac{2}{x - 4}$
Simplify $\frac{x^2 - 8x + 12}{x^2 - 36}$	
Simplify $\frac{2x^2 + 7x - 9}{4x^2 - 81}$	

TRIGONOMETRY



PYTHAGORAS

$$c^2 = a^2 + b^2$$



1. Label the sides

2. Use the formula: $c^2 = a^2 + b^2$

3. Put in the numbers:

$$c^2 = 9^2 + 11^2$$

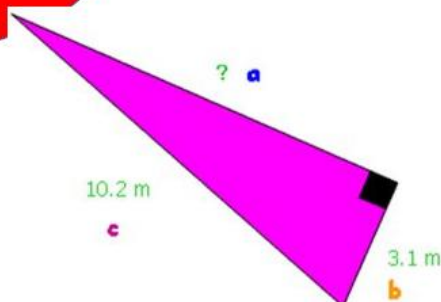
$$c^2 = 81 + 121$$

$$c^2 = 202$$

$$c = \sqrt{202}$$

$$c = 14.2\text{cm (1dp)}$$

Square root
both sides!



1. Label the sides

2. Use the formula: $a^2 = c^2 - b^2$

3. Put in the numbers:

$$a^2 = 10.2^2 - 3.1^2$$

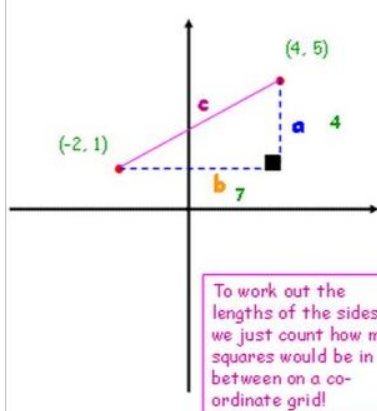
$$a^2 = 104.04 - 9.61$$

$$a^2 = 94.43$$

$$a = \sqrt{94.43}$$

$$a = 9.72\text{m (2dp)}$$

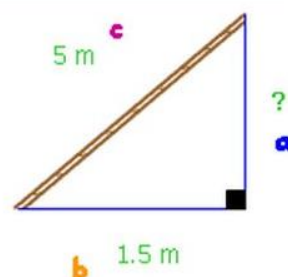
Square root
both sides!



To work out the
lengths of the sides,
we just count how many
squares would be in
between on a co-
ordinate grid!

A 5m ladder rests against the side of a house. The foot of the ladder is 1.5m away from the house. How far up the side of the house does the ladder reach?

PYTHAGORAS



1. Label the sides

2. Use the formula: $c^2 = a^2 + b^2$

3. Put in the numbers:

$$c^2 = 4^2 + 7^2$$

$$c^2 = 16 + 49$$

$$c^2 = 65$$

$$c = \sqrt{65}$$

$$c = 8.1 \text{ (1dp)}$$

Square root
both sides!

1. Label the sides

2. Use the formula: $a^2 = c^2 - b^2$

3. Put in the numbers:

$$a^2 = 5^2 - 1.5^2$$

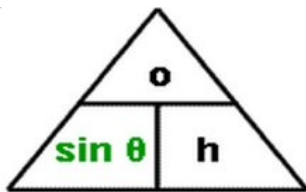
$$a^2 = 25 - 2.25$$

$$a^2 = 22.75$$

$$a = \sqrt{22.75}$$

$$a = 4.77\text{m (2dp)}$$

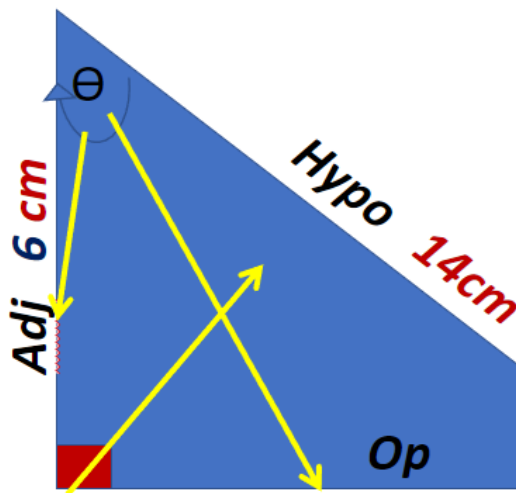
Square root
both sides!



1. Label
2. Information
3. Rule
4. Substitution
5. Work out the answer
6. Round if needed

O A O
S H C H T A

Calculating an angle if
you know two sides



$$2) \theta = x$$

$$A = 6 \text{ cm}$$

$$H = 14 \text{ cm}$$

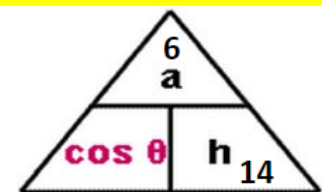
SOH C AH TOA
SOH CAH TOA

$$\cos \theta = \frac{A}{H}$$

$$4) \cos \theta = \frac{6}{14}$$

$$5) \theta = \text{shift Cos } 6/14$$

$$\theta = 64.62306647$$



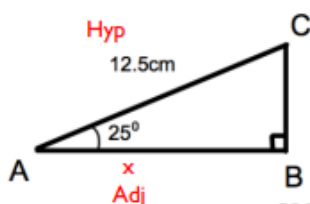
$$6) \theta = 64.6 \text{ cm}$$

$$(3 \text{ SF})$$

What you need to know:

Trigonometry – Finding a side 1

Calculate the length of AB.



- Step 1 – Label the sides you need as O, A or H.
- Step 2 – Use this to decide which trig ratio to use.
- Step 3 – Substitute the given values into the formula.
- Step 4 – Use inverse operations to rearrange & isolate x.

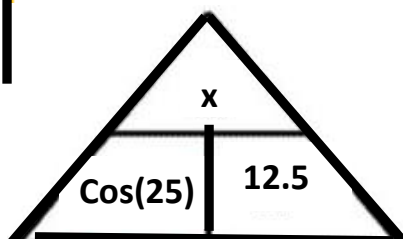
$$\cos(25) = \frac{x}{12.5}$$

$$\cos(25) \times 12.5 = x$$

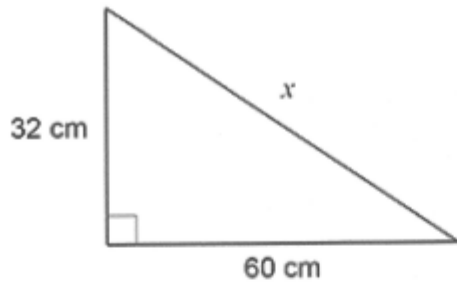
$$x = 11.32884734 \text{ cm}$$

The inverse of
dividing by 12.5 is
multiplying.

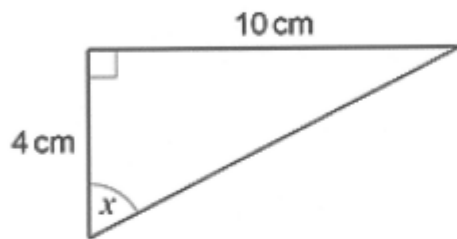
Don't round your
answer, you get no
marks for this!



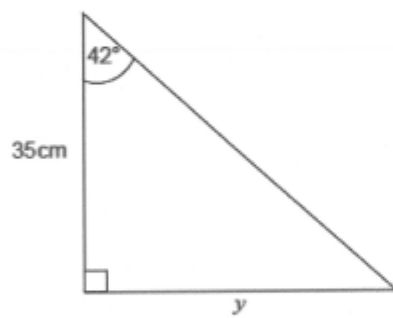
1)



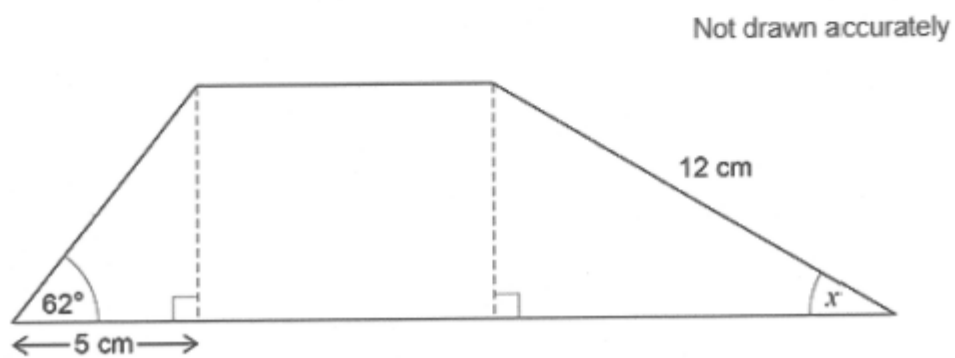
2)





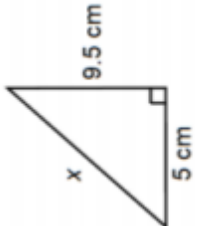
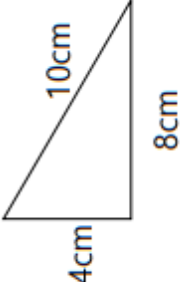

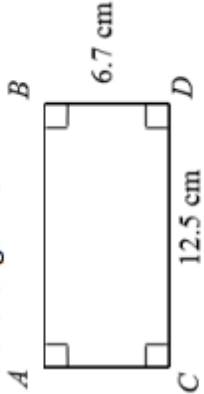
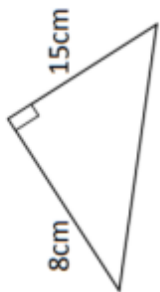
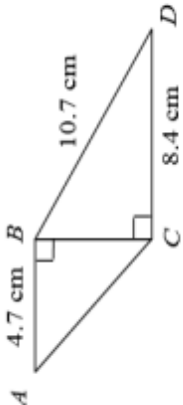
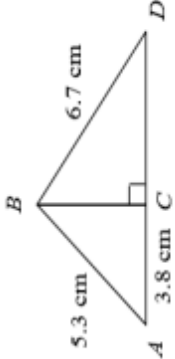
3)



4)



Work out the size of angle x .

<p>1. Use your calculator to work out</p> <p>a) 4.3^2</p> <p>b) $7^2 + 9^2$</p> <p>c) $\sqrt{31.36}$</p>	<p>2. Find the value of x in questions 2-5</p> 	<p>3. Find the value of x in the following</p> 
<p>4.</p> 	<p>5. Is this triangle right-angled?</p> 	<p>6. Find the value of x in the following</p> 
<p>7. Find the length BC</p> 	<p>8. ABC is a right-angled triangle. AB = 15.5 m and AC = 12 m. Find the length of BC. Give your answer to 1 decimal place.</p>	<p>9. Find the perimeter of the following</p> 
<p>10. Find the length AC</p> 	<p>11. Triangle ABC has perimeter 12 m. AB = 5 m and BC = 4 m. Is triangle ABC a right-angled triangle? Show clearly how you decide.</p>	<p>12. Find the length CD</p> 

Yr 11 (H) Revision - Sine Rule

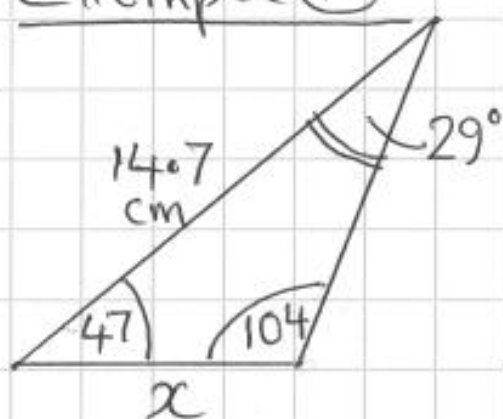
To calculate
a length

$$\frac{a}{\sin(A)} = \frac{b}{\sin(B)}$$

To calculate
an angle

$$\frac{\sin(A)}{a} = \frac{\sin(B)}{b}$$

Example (1)



firstly work out the missing
angle.... $180 - 47 - 104 = \underline{\underline{29}}$

$$\frac{x}{\sin(29)} = \frac{14.7}{\sin(104)}$$

$$x = \frac{14.7}{\sin(104)} \times \sin(29) = \underline{\underline{7.34 \text{ cm}}}$$

Example (2)

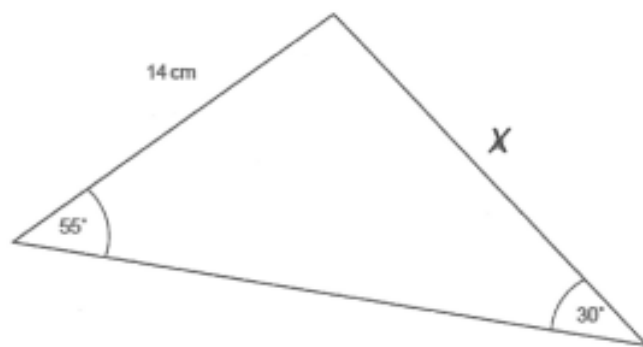


$$\frac{\sin(A)}{8} = \frac{\sin(32)}{6}$$

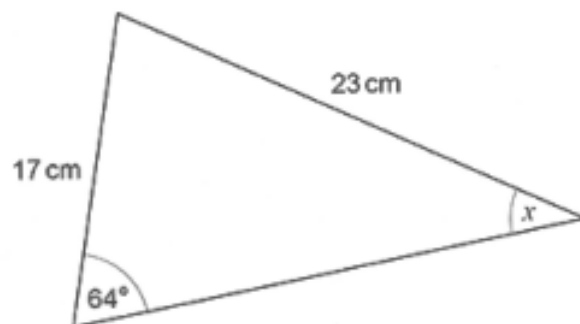
$$\sin(A) = \frac{\sin(32)}{6} \times 8$$

$$\text{then } \sin^{-1}(\text{ANS}) = \underline{\underline{45^\circ}}$$

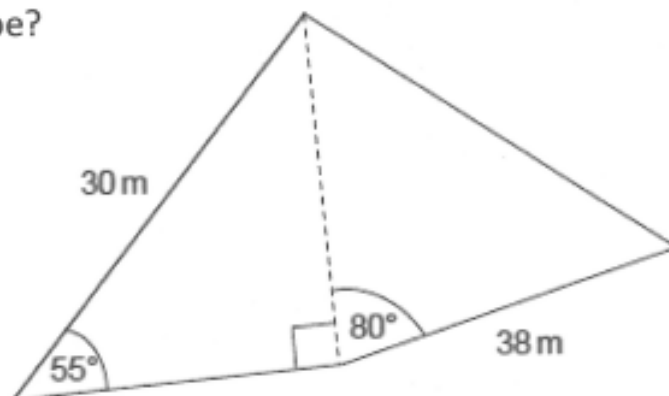
1)



2)

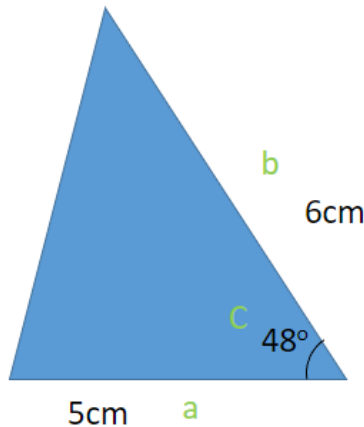


3) Perimeter of shape?



Example – find the area

Learn the formula:- $\text{Area} = \frac{1}{2}ab\sin C$



Find the area of the triangle to 1dp.

1) Label sides

2) Substitute in values:

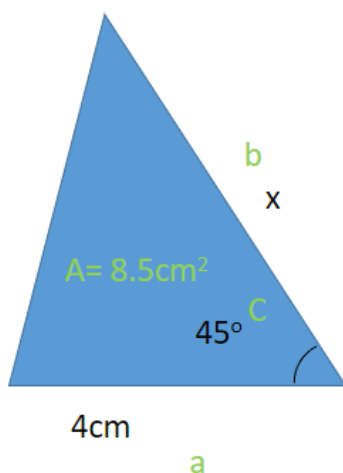
$$\text{Area} = \frac{1}{2} \times 5 \times 6 \times \sin(48)$$

3) Type in to your calculator:

11.1cm to 1dp

Example – missing side

Learn the formula:- $\text{Area} = \frac{1}{2}ab\sin C$



Find the length of 'x' 1dp.

1) Label sides

2) Substitute in values:

$$8.5 = \frac{1}{2} \times 4 \times ? \times \sin 45$$

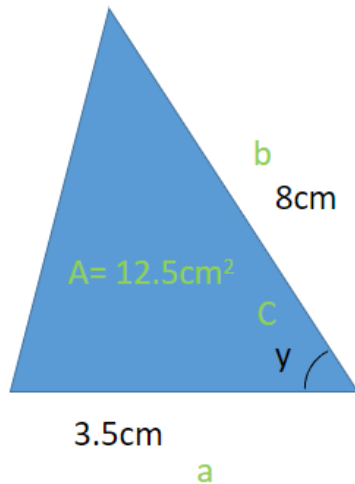
3) Divide through by everything except the ?.

$$\frac{8.5}{\frac{1}{2} \times 4 \times \sin 45} = ?$$

4) Type in to calculator: 6.0cm to 1dp

Example – missing angle

Learn the formula:- $\text{Area} = \frac{1}{2} ab \sin C$



Find the length of 'y' 1dp.

1) Label sides

2) Substitute in values:

$$12.5 = \frac{1}{2} \times 3.5 \times 8 \times \sin(?)$$

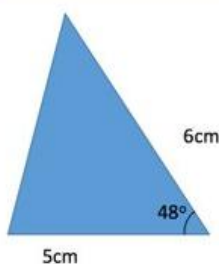
3) Divide through by everything except the sin(?).

$$\frac{12.5}{\frac{1}{2} \times 3.5 \times 8} = \sin(?)$$

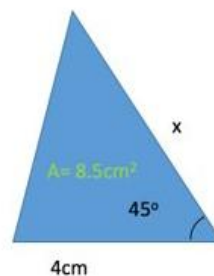
4) Type in to calculator and don't forget to \sin^{-1} : **62.3° to 1dp**

Area = $\frac{1}{2} ab \sin C$

Find the **area**



Find the **missing side**



Find the **missing angle**

