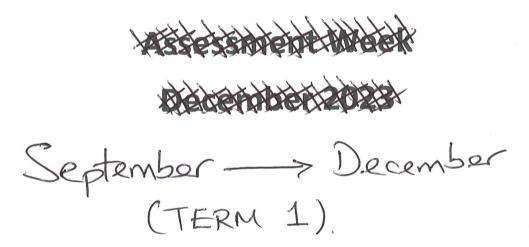
Year 11 (HIGHER)

GCSE Maths

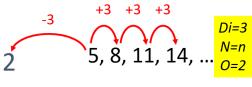
Revision Pack



| Name | Form |
|------|------|
| | |

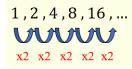
Number Sequences (ALL)

Linear



3n + 2

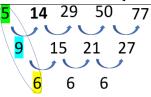
Geometric

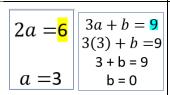


 $64, 16, 4, 1, \frac{1}{4}, \frac{1}{16}$

Multiply or divide by the same number

Quadratic



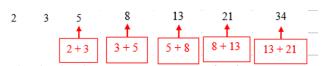


$$a + b + c = 5$$

 $3 + 0 + c = 5$
 $c = 2$

Fibonacci

RULE: Fibonacci sequence: the next term in the sequence is the sum of the two previous terms.



Find the first 6 terms of the Fibonacci sequence:

$$a, b, a + b$$

The 4th term: b + a + b = a + 2bThe 5th term: a + b + a + 2b = 2a + 3bThe 6th term: a + 2b + 2a + 3b = 3a + 5b

a, b, a + b, a + 2b, 2a + 3b, 3a + 5b

Sequences

10, 7, 4, 1,

2, 5, 10, 17, 26

- 13, 22, 31, 40,
- -10, -13, -16, -19,
- 3, 14, 29, 48, 71
- 2) Continue the following geometric sequences:
- a) 1, 2, 4, 8, ,
- b) 5, 50, 500, 5000,, ,
- c) 3, 9, 27, 81, ,
- d) 4, 20, 100, ,
- e) 4, 16, 64, ,
- f) 64, 32, 16, 8, 4, ,

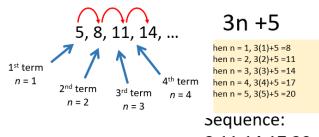
Find the next three terms of the following Fibonacci-style sequences

- (a) 2, 4, 6, 10, ...
- (b) 3, 6, 9, 15, ...
- (c) 4, 8, 12, 20, ...
- (d) 15, 23, 38, 61, ... (e) 5, 12, 17, 29, ...
- $(f) -3, 5, 2, 7, \dots$

For each of the following Fibonacci-style sequences, find the next 4 terms.

- (a) $a, 4a, 5a, 9a, \dots$
- (b) 3x, 3x + y, 6x + y, 9x + 2y, ...
- (c) $6a, -2a, 4a, 2a, \dots$
- (d) 2y, y + z, 3y + z, ...
- (e) 4x 5y, 2x y, 6x 6y, ... (f) -x, x + y, y, ...

Examples – generating sequences



When n = 1,
$$2(1^2) - 3 = -1$$

When n = 1, $2(2^2) - 3 = 5$
When n = 1, $2(3^2) - 3 = 15$
When n = 1, $2(4^2) - 3 = 29$
When n = 1, $2(5^2) - 3 = 47$

 $2n^2 - 3$

8,11,14,17,20

Sequence: -1,5,15,29,47

Questions - generating sequences

The nth term for some sequences are given below. Find the first 5 terms for each sequence.

5n + 3(a)

- (b) 2n + 9
- (c) 3n - 2

- 10n 6 (d)
- 9n + 10(e)
- (f) n + 8

- -7n + 20(g)
- 50 5n (h)
- (i) 3.5n + 4

For each nth term, work out the first five terms of the sequence.

- (a) $n^2 + n$
- (b) $n^2 + 2n$ (c) $n^2 n$
- (d) $n^2 3n$

- (e) $n^2 + n + 2$ (f) $n^2 2n + 5$ (g) $n^2 + 4n 10$ (h) $2n^2 + n$

- (i) $3n^2 n + 6$ (j) $10n^2 + 5n 7$

Yr II (H) Revision - Iteration. Example (1) Solve x3-8x-10=0 3dp Step 1 Make the "2" with the largest power, the subject $ie- x = \sqrt{10 + 8x}$ Step 2 Given that 70 = 3, solve. Substitute x=3 into \$10+8x 20=3 gives 3.239611... Now sub. x = 3.239611 into etc. $\chi_0 = 3$ $\chi_1 = 3.239611$ 2 = 3.29938 73-3-31396 24 = 3.31749 & toop going 26 = 3.31846 $2C_5 = 3.31835$

Use the iteration
$$x_{n+1} = \sqrt{\frac{2x_n + 4}{5}}$$

to work out an approximate solution to

$$x = \sqrt{\frac{2x+4}{5}}$$

Start with $x_1 = 1$

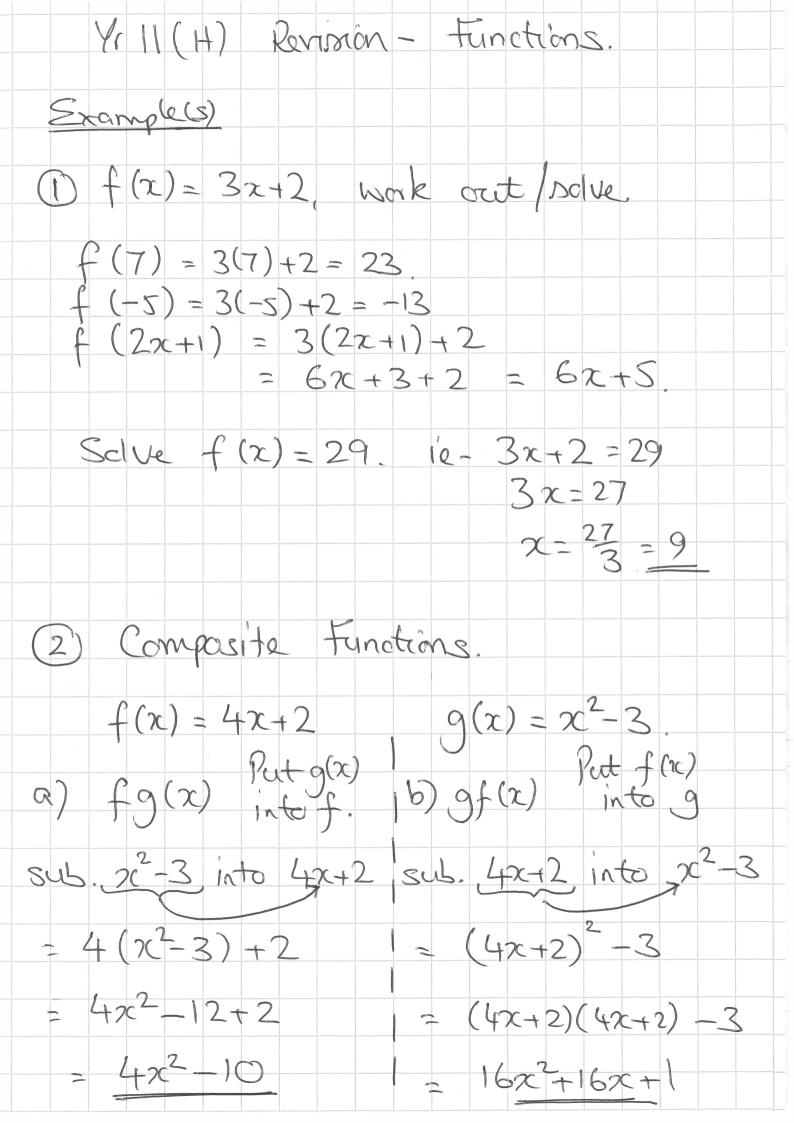
Give your answer to 2 decimal places.

2)
$$x_{n+1} = \sqrt[3]{3x_n + 7}$$

Use a starting value of $x_1 = 2$ to work out a solution to $x = \sqrt[3]{3x+7}$ Give your answer to 3 decimal places.

3)

Show that the equation $x^3 + 8x = 30$ has a solution between x = 2.2 and x = 2.3



1a) For all values of
$$x$$
, $f(x) = 2x^2 + 3$ $g(x) = x + 4$

(a) Show that
$$fg(x) = 2x^2 + 16x + 35$$

1b) (b) Solve
$$fg(x) = gf(x)$$

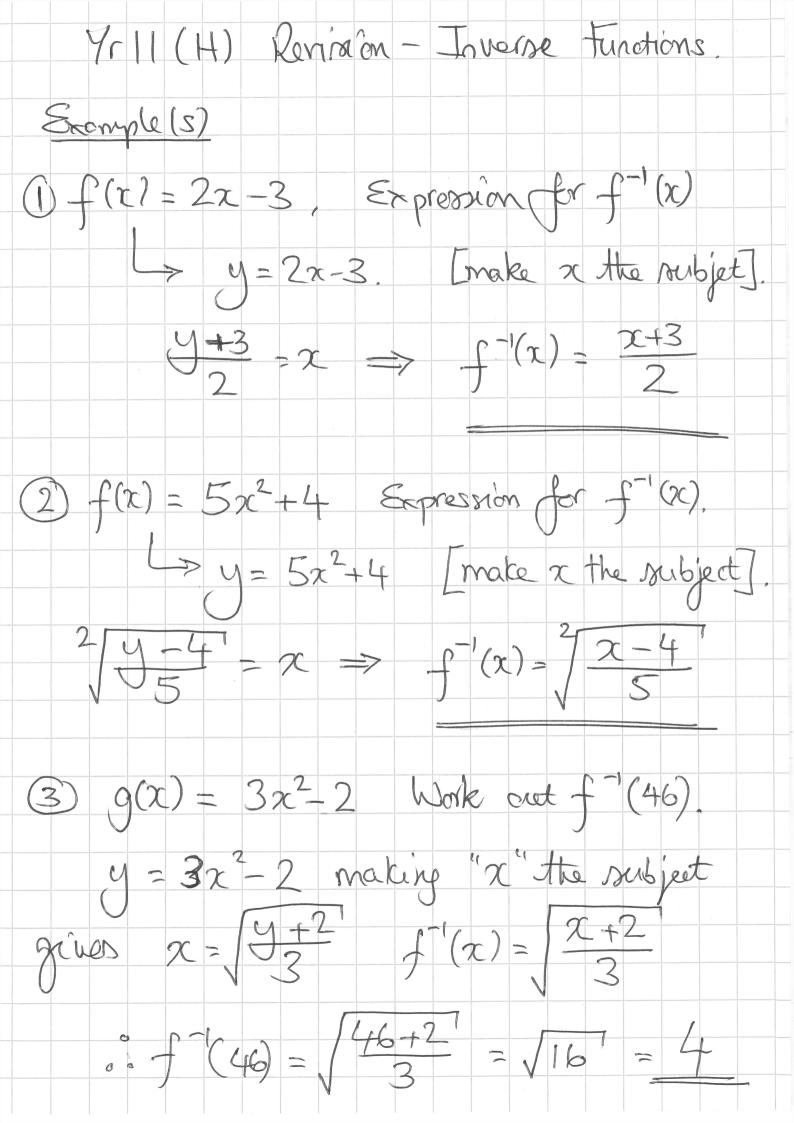
2)
$$f(x) = 3^x$$
 and $g(x) = 3x + 7$

(a) Work out the value of
$$f(2) + g(5)$$

3)
$$f(x) = 2x^2$$

 $g(x) = x + 5$

Work out the composite function fg(x)



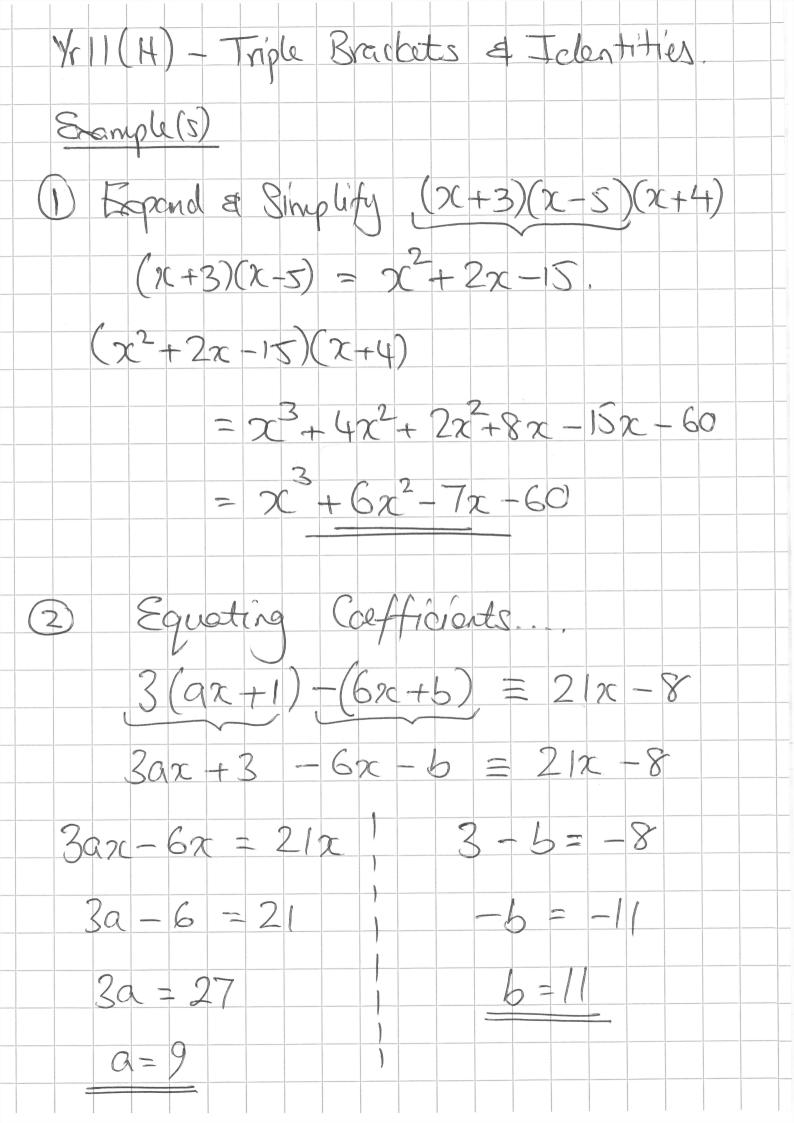
1)
$$f(x) = \frac{3x+9}{5}$$
 Show that $f^{-1}(8)$ is **not** an integer.

2)
$$f(x) = 2x + 5$$

Show that
$$3f(x) - 12f^{-1}(x)$$
 simplifies to an integer.

For all values of
$$x$$
, $f(x) = \frac{9x+4}{7}$

Work out $f^{-1}(x)$

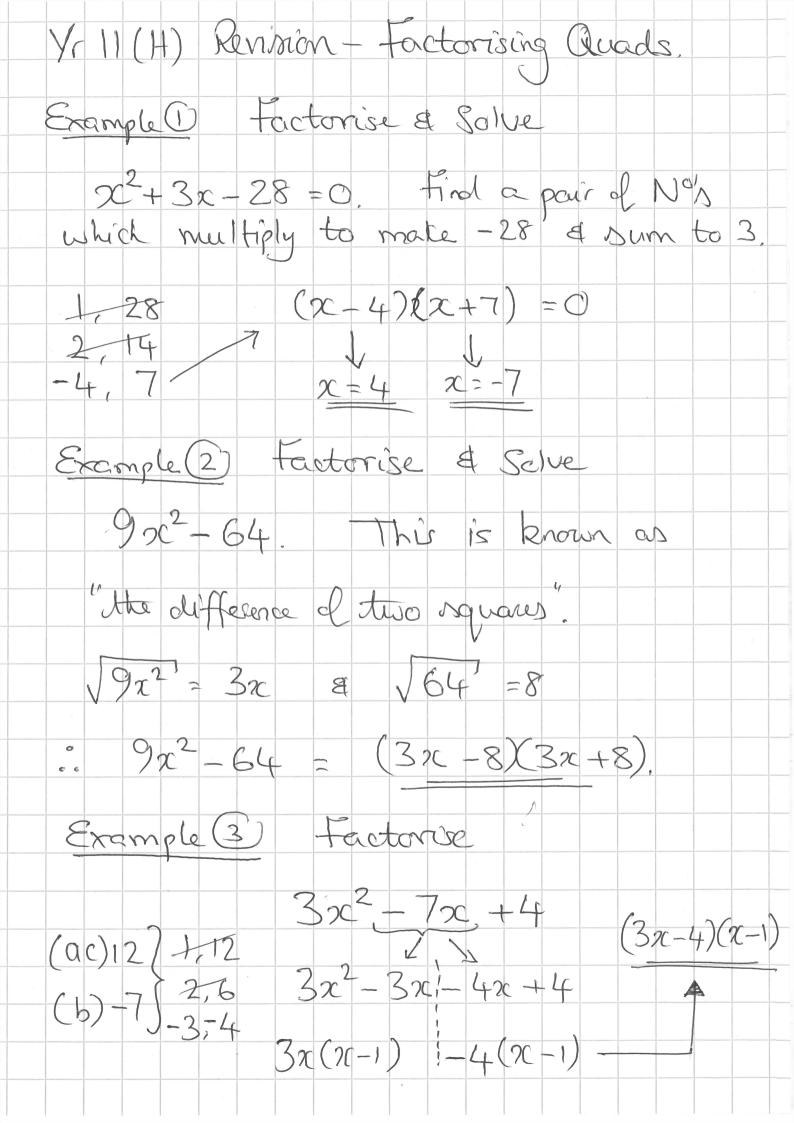


1) Show that $(3x + 4)(2x - 5) - 11x(x - 2) + 5(x^2 - 3x - 1)$ simplifies to an integer.

2) Expand and simplify fully (x-3)(x-4)(x+8)

3)
$$(5x + 2)(x - 3) + ax + b \equiv 5x^2 - 16x + 7$$

Work out the values of a and b

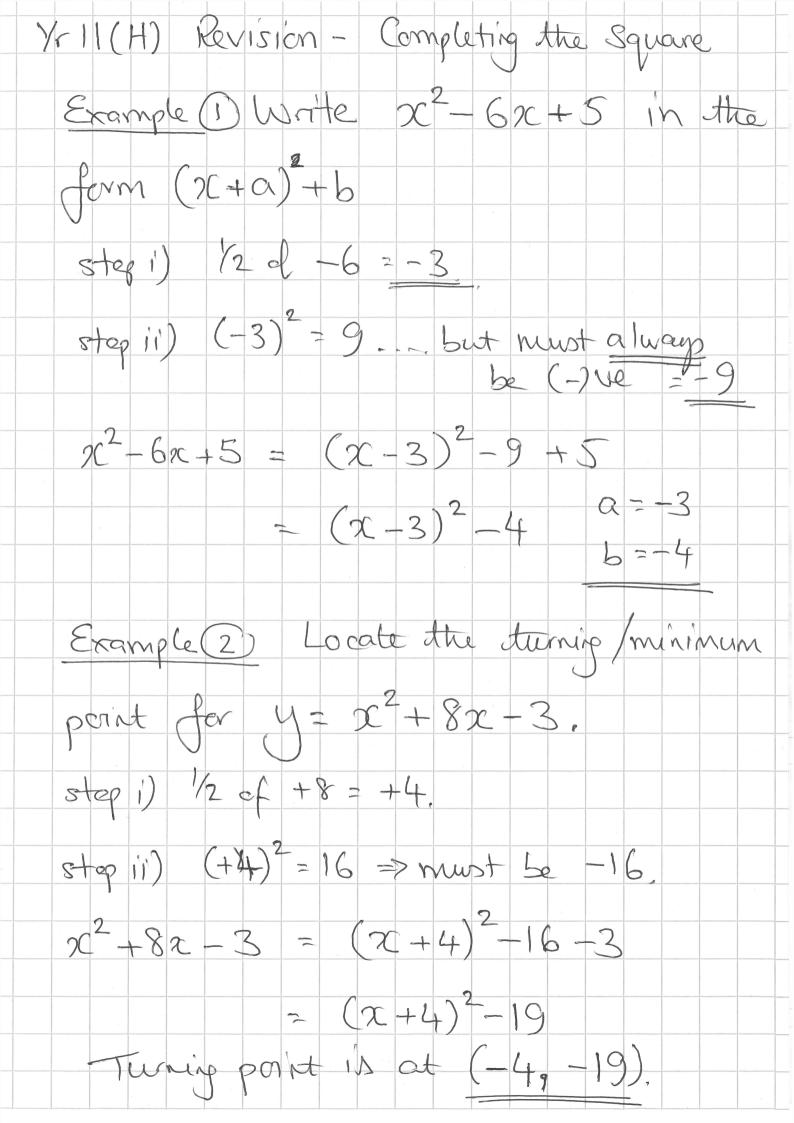


(a) Factorise
$$5x^2 + 6x - 8$$

(b) Simplify fully
$$\frac{x^2 + 9x + 14}{x^2 - 4}$$

2) Factorise fully
$$2x^2 - 50y^2$$

3) Simplify
$$\frac{3x^2 - 19x + 20}{x^2 - 25}$$



Write
$$x^{2} + 10x + 28$$
 in the form $(x + a)^{2} + b$

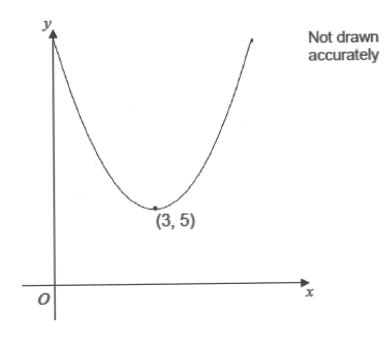
$$(x+a)^2+b$$

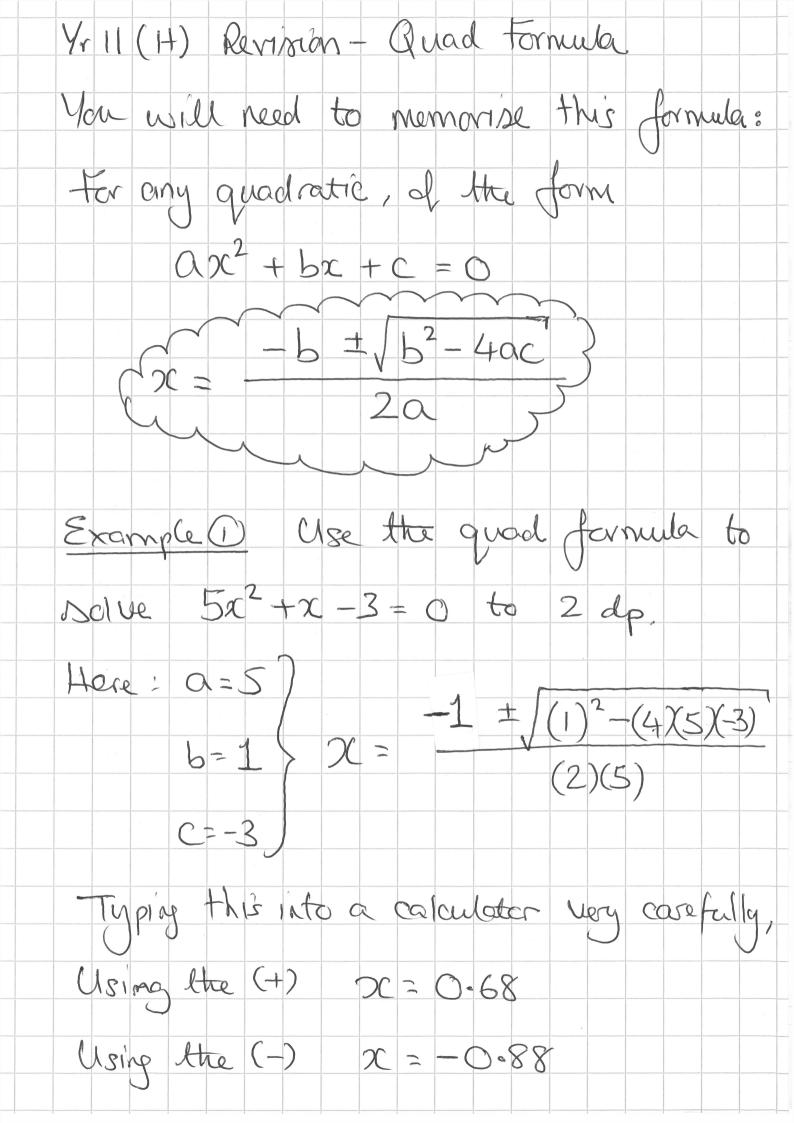
The equation of a curve is $y = (x + 3)^2 + 5$ 2) Circle the coordinates of the turning point.

$$(-3, 5)$$

3) Write $x^2 - 10x + 29$ in the form $(x - a)^2 + b$

- A sketch of $y = x^2 + cx + d$ is shown. 4)
 - The turning point is (3, 5)





Using the quadratic formula, or otherwise, solve
$$3x^2 + x - 5 = 0$$

$$3x^2 + x - 5 = 0$$

2) Solve
$$4x^2 + 7x - 3 = 0$$

Give your answers to 2 decimal places.

Solve
$$\frac{5}{4x+1} = \frac{2x}{x^2+3}$$

Give your solutions to 3 significant figures.

To enlarge a shape or describe an enlargement you need these two details:

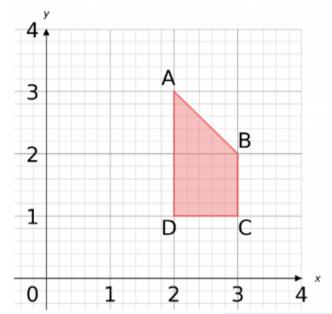
- The Scale factor (Scale factor = $\frac{\text{New Length}}{\text{Old Length}}$)
- The centre of enlargement (co-ordinates)

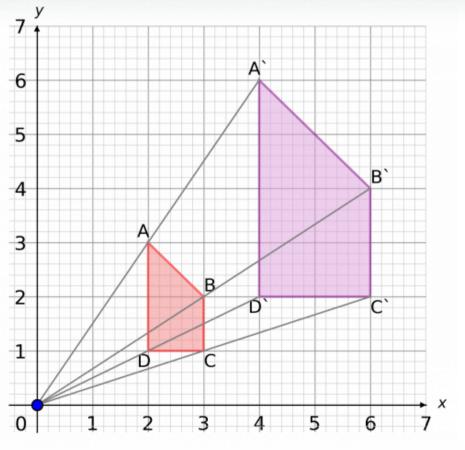
Example: Enlarge shape ABCD below by scale factor ${\color{red}2}$ about the origin.

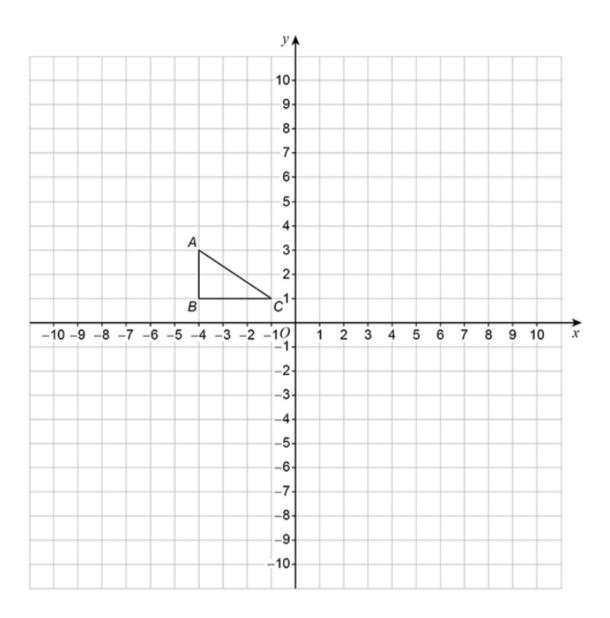
The **centre of enlargement** is the origin (0,0)

The Scale factor is 2









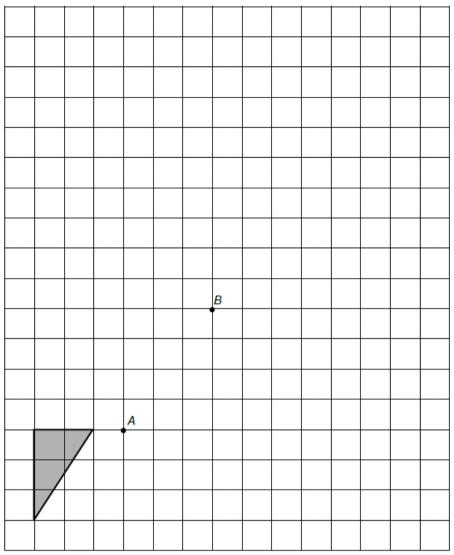
ABC is transformed to A'B'C' by a reflection in the line x = 1A'B'C' is transformed to A"B"C" by a rotation 90° anticlockwise about (1, -4)Which **one** point on ABC is invariant under the combined transformation?

You **must** show the result of each transformation on the grid.

The shape is **rotated** 180° about point A.

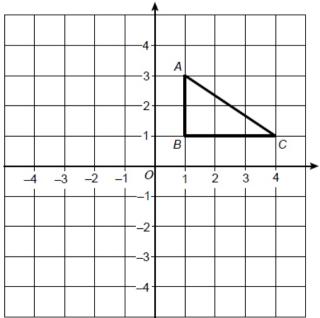
It is then **enlarged** by scale factor -2, centre B.

Draw the final shape on the diagram.



2)

(a) Here is triangle ABC.



Describe fully a **single** transformation of the triangle for which all points on *AB* are invariant there are no other invariant points.

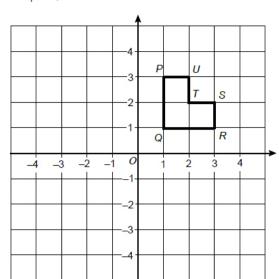
3)

Describe fully a single transformation of the L-shape for which

Q is invariant

the line joining ${\it P}$ and ${\it Q}$ becomes horizontal

the area of the L-shape does not change.



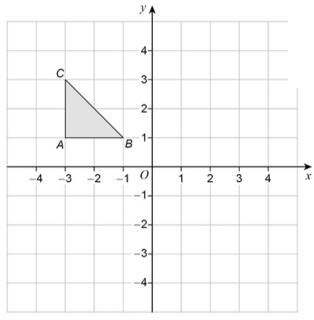
4) Here is triangle ABC on a grid.



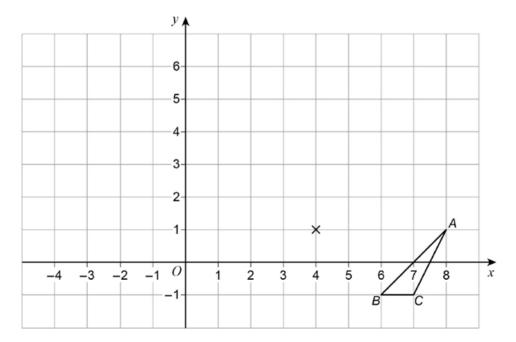
point B is invariant

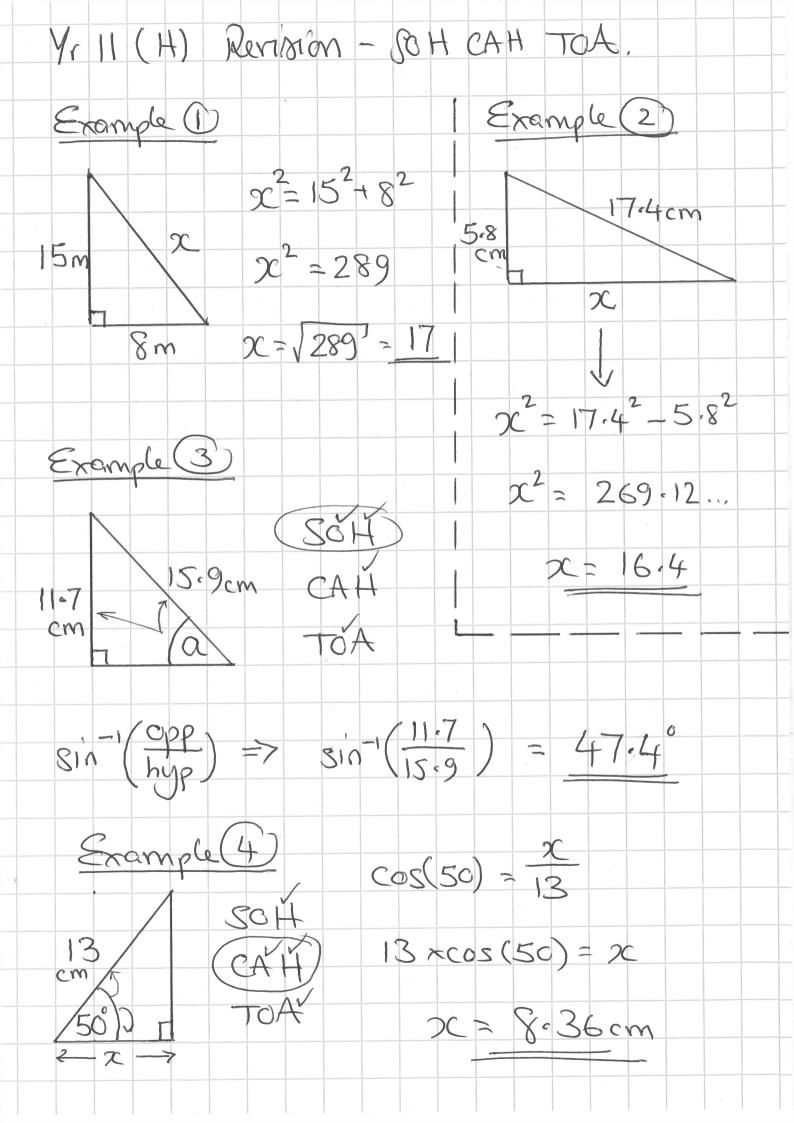
point A moves to (1, 1)

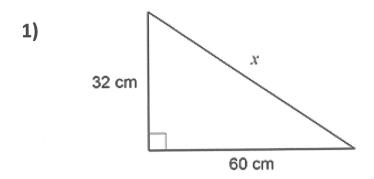
point C moves to (1, -1)

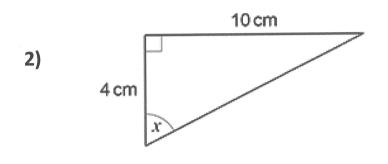


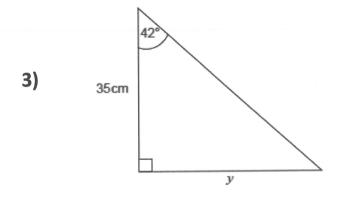
5) Enlarge triangle ABC by scale factor –2, centre (4, 1)

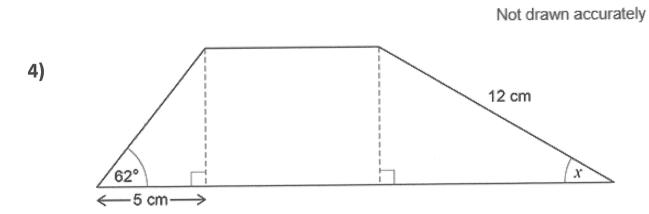






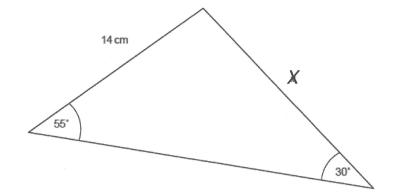




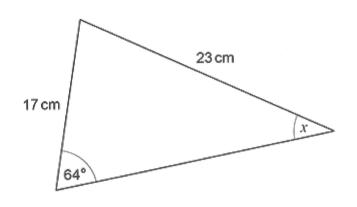


Work out the size of angle x.

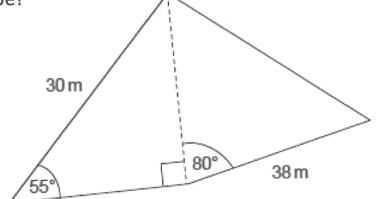
Yr II (H) Revision - Sine Rule To calculate $Sin(A) = \frac{b}{sin(B)}$ a length sin(A) = sin(B) a = b.To calculate an angle firstly work out the missing Example (1) 180-47-104=29 $\frac{2}{\sin(29)} = \frac{14.7}{\sin(104)}$ 47) 104 $90 = \frac{14.7}{\sin(104)} \times \sin(29) = 7.34$ cm Example (2) $\frac{\sin(A)}{8} = \frac{\sin(32)}{6}$ Sem $Sin(A) = \frac{sin(32)}{6} \times 8.$ then sin- (ANS) = 45°

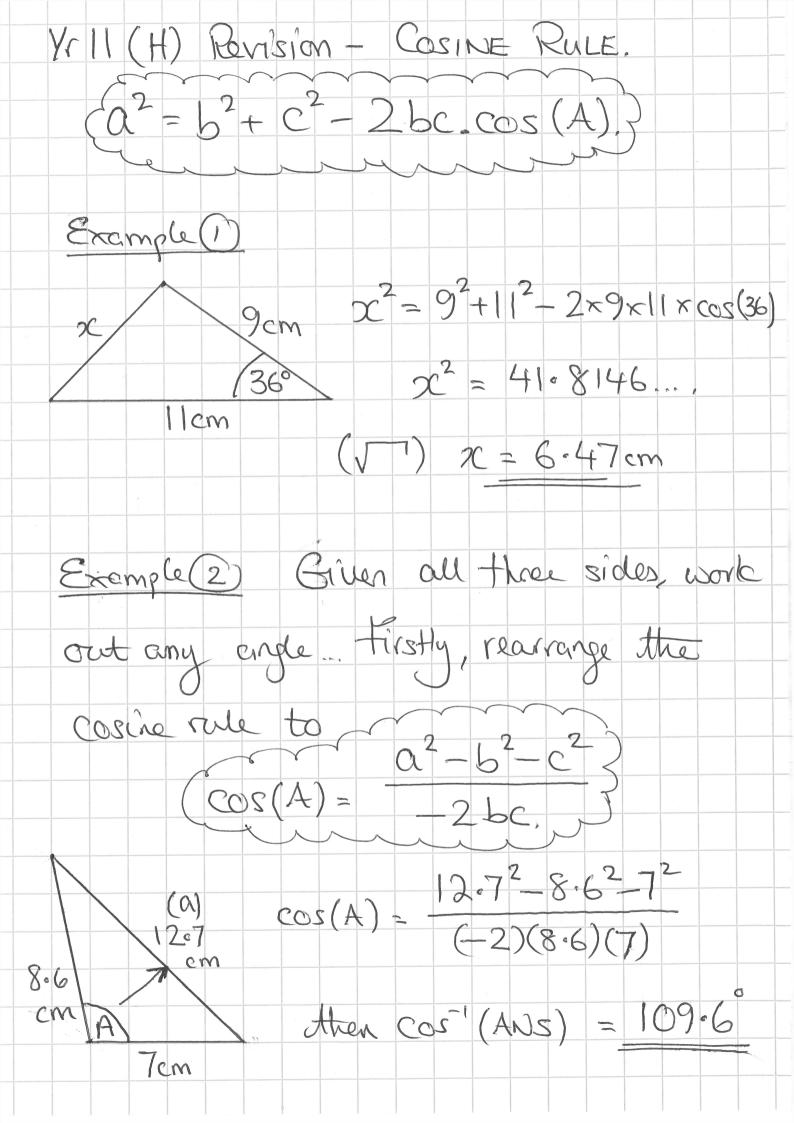


2)

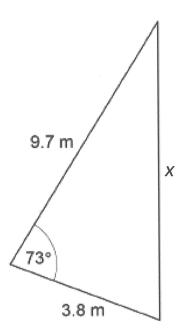


3) Perimeter of shape?



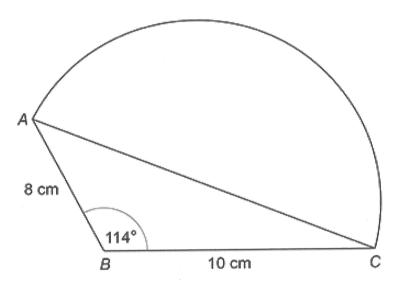


Work out length x



2) A shape is made by joining triangle ABC to a semicircle with diameter AC.

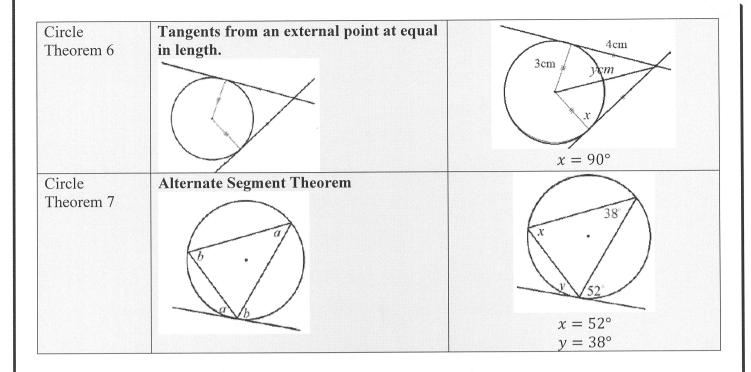
Not drawn accurately



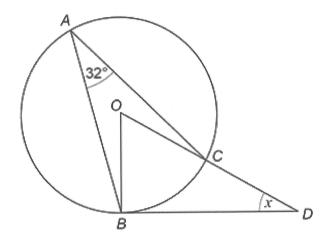
Work out the total area of the shape.

Topic: Circle Theorems

| Topic/Skill | Definition/Tips | Example |
|---------------------|---|---|
| Circle Theorem 1 | Angles in a semi-circle have a right angle at the circumference. | $y = 90^{\circ}$ $x = 180 - 90 - 38 = 52^{\circ}$ |
| Circle Theorem 2 | Opposite angles in a cyclic quadrilateral add up to 180° . $a + c = 180^{\circ}$ $b + d = 180^{\circ}$ | $x = 180 - 83 = 97^{\circ}$ $y = 180 - 92 = 88^{\circ}$ |
| Circle Theorem 3 | The angle at the centre is twice the angle at the circumference. | $x = 104 \div 2 = 52^{\circ}$ |
| Circle Theorem 4 | Angles in the same segment are equal. | $x = 42^{\circ}$ $y = 31^{\circ}$ |
| Circle Theorem 5 | A tangent is perpendicular to the radius at the point of contact. | y = 5cm (Pythagoras' Theorem) |

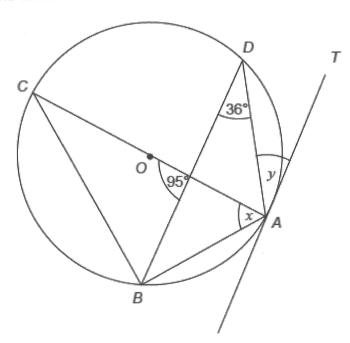


A, B and C are points on a circle, centre O. BD is a tangent to the circle. OCD is a straight line.



Work out the size of angle x.

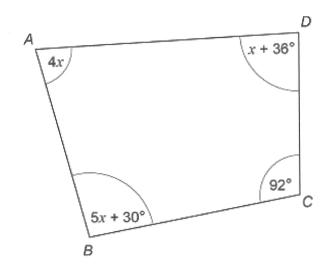
A, B, C and D are points on a circle, centre O.
AC is a diameter of the circle.



AT is a tangent to the circle.

Work out the size of angle \boldsymbol{x} and the size of angle \boldsymbol{y}

Not drawn accurately

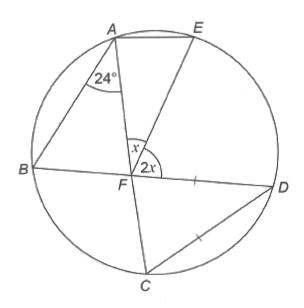


Prove that ABCD is **not** a cyclic quadrilateral.

4) A, B, C, D and E are points on a circle.

BFD and AFC are straight lines.

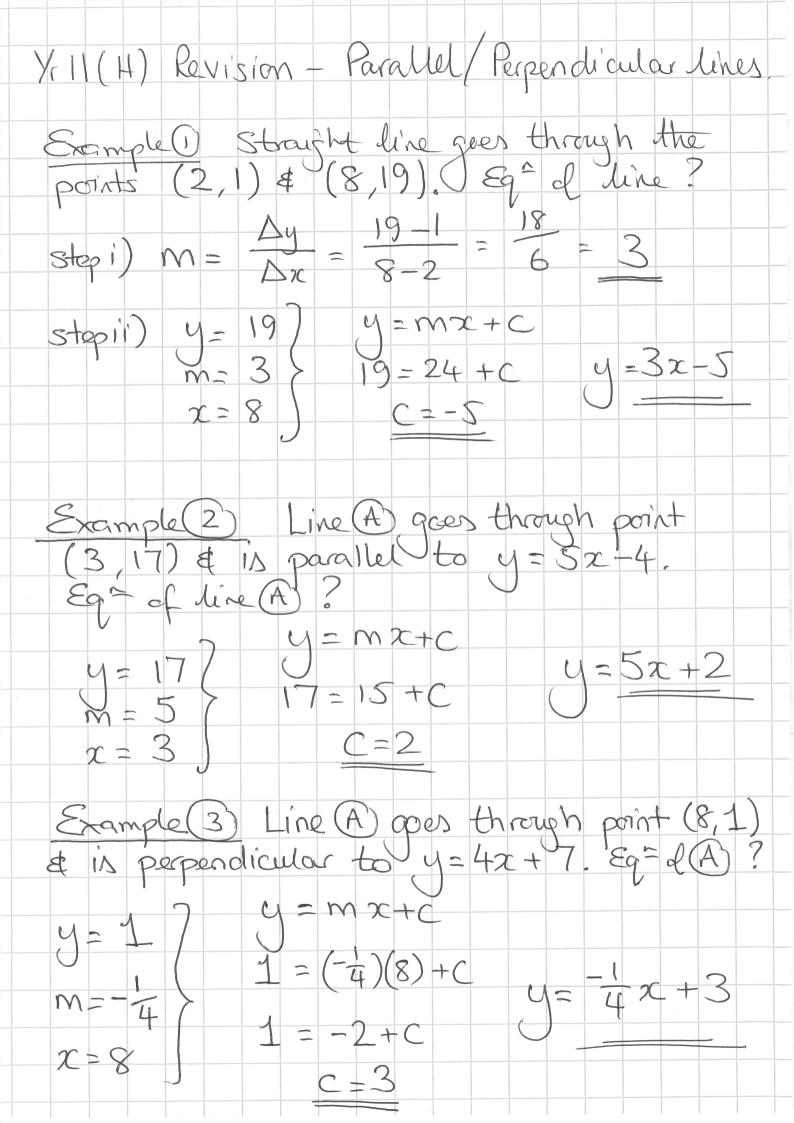
DC = DF



Not drawn accurately

Work out the size of angle x.

You must show your working which may be on the diagram.



is parallel to the line

v = 4x - 1 and passes through

(-1, 1)

2) A straight line

is perpendicular to the straight line through (2, 8) and (6, 15)

and

passes through (0, 9) and (x, 17)

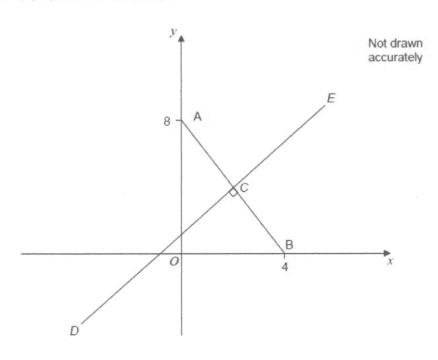
Work out the value of x.

ACB is a straight line.

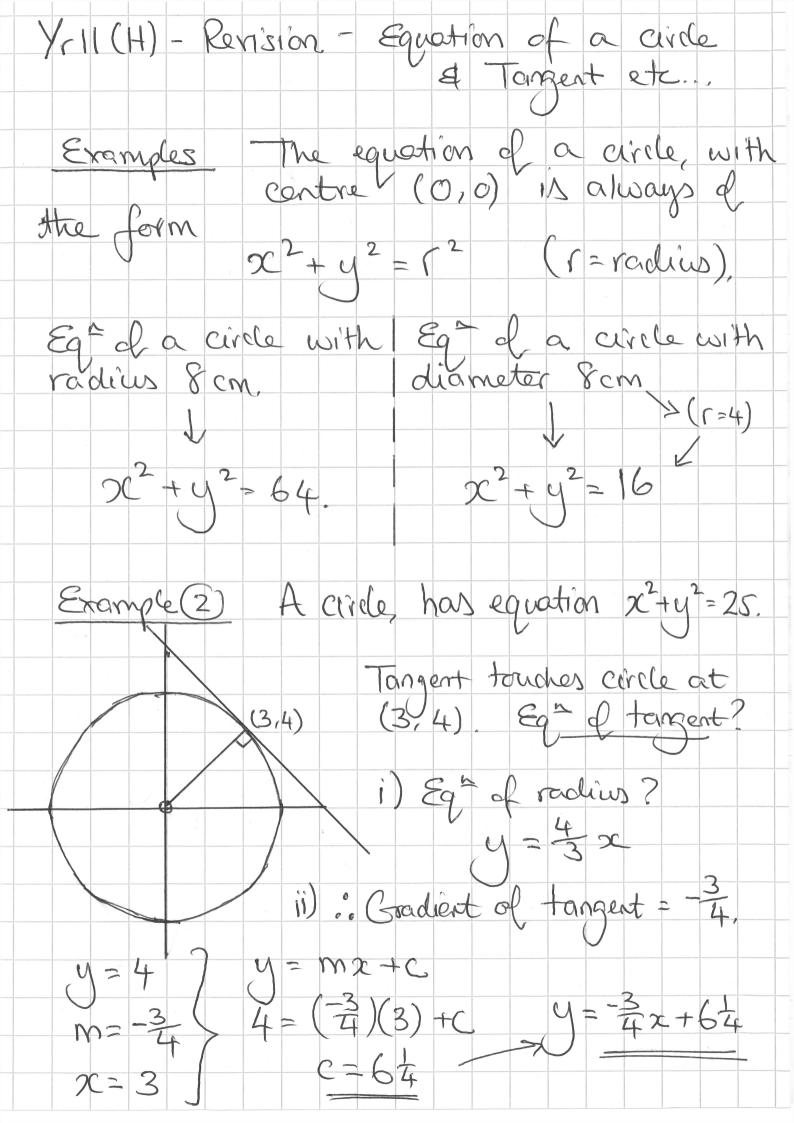
A is the point (0, 8), and B is the point (4, 0)

C is the midpoint of AB.

Line DCE is perpendicular to line ACB.



Work out the equation of line DCE.



1) Which of these is the equation of a circle? Circle your answer.

$$x^2 - y^2 = 6$$
 $x^2 + y^2 = 6$

$$x^2 + y^2 = 6$$

$$y = x^2 - 6$$

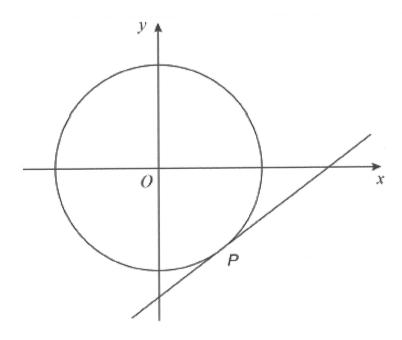
$$y = x^2 + 6$$

2) A circle has equation $x^2 + y^2 = 25$

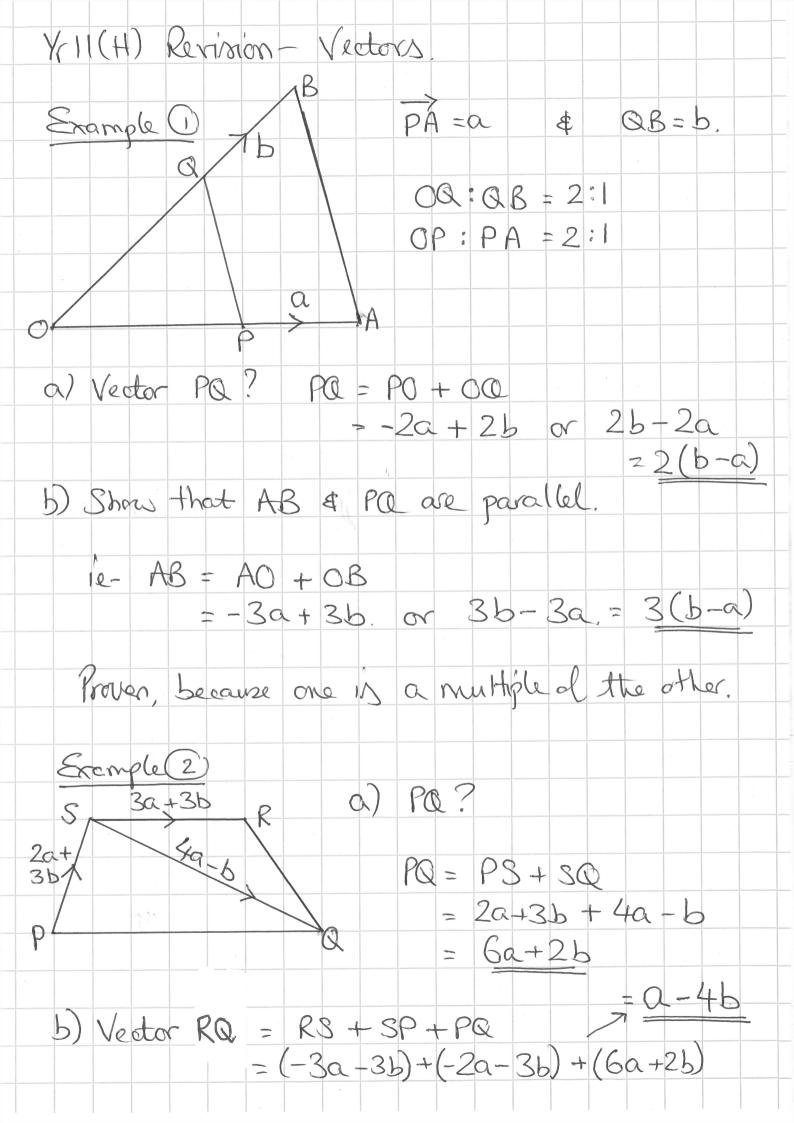
Work out the length of its radius.

3) *P* is a point on the circle with equation $x^2 + y^2 = 80$

P has x-coordinate 4 and is below the x-axis.



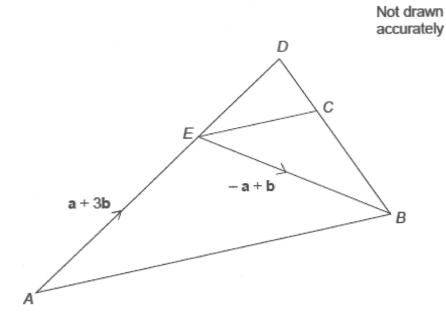
Work out the equation of the tangent to the circle at P.



AED is a straight line.

$$\overrightarrow{AE} = \mathbf{a} + 3\mathbf{b}$$

$$\overrightarrow{EB} = -\mathbf{a} + \mathbf{b}$$



- (a) Work out the vector \overrightarrow{AB}
- (b) Also $\overrightarrow{ED} = \frac{1}{3} \overrightarrow{AE}$ and $\overrightarrow{DC} = -\frac{1}{3} \mathbf{a}$

Prove that EC is parallel to AB.

2)

